Bidimensional Instability in Antiferroelectric Liquid Crystals

M. Becchi^{1,2}, S. Ponti^{1,2}, A. Strigazzi^{1,2}, V. Chigrinov^{3,4}, and S. Torgova^{2,5}

¹ Dipartimento di Fisica and I.N.F.M., Politecnico di Torino,

Corso Duca degli Abruzzi 24, I-10129 Torino, Italy

 2 Joint Laboratory of Orientationally Ordered Media (OOM-Lab),

C. Duca degli Abruzzi 24, I-10129 Torino, Italy

 3 Institute of Crystallography, Leninski pr. 52, Moscow, Russia

⁴ Hong Kong University of Science and Technology, China

 5 SSC RF "NIOPIK" (Organic Intermediates & Dyes Institute),

B. Sadovaya 1/4, Moscow 103787, Russia

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In the last decade it has been experimentally found a periodic domain pattern arising in smectic C^* liquid crystals in surface stabilized bookshelf geometry. Such a periodic texture appears after switching-off an external electric field, even in strong anchoring conditions. It has a static character and can be bidimensional, being dependent on both directions normal to the smectic planes and normal to the cell plates. In the present work an explanation to this phenomenon is proposed. According to our model in the antiferroelectric phase the biperiodic texture is a threshold phenomenon, appearing for values of the spontaneous polarization greater than a critical value, whereas in the ferroelectric phase this type of bidimensional instability is hindered.

I Introduction

The importance of Ferroelectric Liquid Crystals (FLC) is strictly related to the nonlinear electro-optic effect determined by the coupling of the spontaneous polarization \overrightarrow{P}_s with an external applied electric field \overrightarrow{E}_{ext} [1]. The effect can be characterized by bistability and optical memory in the surface stabilized bookshelf [2, 3] or quasi bookshelf [4] configuration. In this case, each single layer exhibits a uniform spontaneous polarization, oriented in the same way in the whole cell (see Fig.1 a).

But some smectic C* materials, like MHPOBC, due to their molecular structure [5] can present also a dual arrangement, in which consecutive layers naturally have alternative sense of \vec{P}_{s} - antiferroelectric phase (AFLC). In this state the whole cell spontaneous polarization vanishes. An AFLC under applied electric field can move towards other two stable states, up- and down- via an azimuthal rotation $\delta \phi = \pm \pi$ of alternate layers (see Fig.1 b), allowing to obtain a tristability behaviour [3]. In the last decade, the appearance of static modulated pattern was observed, both in ferroelectricand in antiferroelectric phase [6]-[12], for instance after switching off a DC field applied to a uniform surface stabilized cell. Regular periodic domains occur in this case as static stripes, oriented either parallel [8-11] or perpendicular [6, 7, 12] to the smectic layers normal, which lies in a plane parallel to the cell walls (see Fig. 2).

Up to now several qualitative models describe the possible role played by the presence of a periodic disclination array [13], by flexoelectricity and charge conduction [12].

The purpose of the present paper is to investigate a new mechanism, explaining the biperiodic instability as the result of a competition between the polarizationfield coupling and the coulombian interaction between the polarization charges in the smectic layers. This competition is driven by the anchoring, mediated by the bulk elasticity [14], biased by the dielectric contribution and corrected by the flexoelectricity [15].

II Theory

Let us consider a bookshelf arrangement of a material exhibiting both ferroelectric - and antiferroelectricphases, like MHOPBC. The cell reference frame [x, y, z]has x-axis normal to the cell walls, y-axis parallel to the the glass plates and to the smectic planes, z-axis normal to the smectic planes (see Fig. 1a). \hat{n} is the molecular



Figure 1. Surface stabilized C^* liquid crystal cell with strong anchoring in bookshelf geometry (a). The cell volume is $D_x D_y D_z$, d is the smectic layer thickness. The smectic cone is also reported in (b), with azimuth ϕ , polar angle θ and spontaneous polarization \vec{P}_S either parallel or antiparallel to the unit vector $\hat{p} = \hat{c} \times \hat{k}$, according to the type of molecular chirality.





Figure 2. Periodic distortion modes with wave-vector along the x-axis, normal to the cell plates (a), and along the zaxis, normal to the smectic planes (b). In the case of strong anchoring, the first mode has wavelength λ_x equal to the double of the cell thickness D_x .

director, and \hat{c} is the tilt director. θ is the polar angle characterizing the tilt cone, whereas ϕ is the azimuth of the \hat{n} -director orientation (see Fig. 1b). Any variation $\delta\theta$ is connected with a hard distortion, hindered at constant temperature; instead, any variation $\delta \phi$ is allowed, describing a soft distortion. The LC spontaneous polarization $\overrightarrow{P}_s = P_s \widehat{p}$, where $\widehat{p} = \widehat{c} \times \widehat{k}$ (\widehat{k} is parallel to the z-axis), lies in the smectic layer parallel to xy-plane. The initial configuration of \hat{c} is parallel to y-axis ($\phi_0 = \pi/2$). By applying an external electric field \vec{E}_{ext} along z the linear coupling with the polariza-tion \vec{P}_s produces a certain azimuthal rotation $(\phi - \phi_0)$. After switching off the field, the \hat{c} -distribution relaxes to a configuration different with respect to the previous one. The new configuration is biperiodically distributed in zx-plane, being invariant along y-axis. To describe the modulated pattern, it is convenient to define

$$\phi = \phi_0 + \varphi(x, z) \tag{1}$$

where the wave amplitude $|\varphi| \ll \phi_0$. Moreover, the tilt-director \hat{c} is given by

$$\widehat{c} = -\sin\phi\,\widehat{i} + \cos\phi\,\widehat{j} \simeq -[\sin\phi_0 + \varphi\cos\phi_0]\,\widehat{i} + [\cos\phi_0 - \varphi\sin\phi_0]\,\widehat{j}.$$
(2)

The free energy density of the whole cell accounts for the following contributions:

 $Elastic\ term$

The elastic energy involved in a distortion, where any curvature of smectic plane is prohibited, is given by [16]:

$$f_{el} = \frac{1}{2} [B_1 \sin^2 \phi_0 + B_2 \cos^2 \phi_0] \varphi_x^2 + \frac{1}{2} B_3 \varphi_z^2 - B_{13} \sin \phi_0 \varphi_x \varphi_z, \qquad (3)$$

where $\varphi_x \equiv \partial \varphi / \partial x, \varphi_z \equiv \partial \varphi / \partial z$ and B_i and B_{13} are smectic elastic constants. More precisely, B_1 describes the bend of smectic director \hat{c} , B_2 the splay of smectic director \hat{c} , B_3 the twist of smectic director \hat{c} , and B_{13} is a mixed bend-twist of the nematic director \hat{n} , which vanishes in one-constant approximation [3].

Flexoelectric term

The flexoelectric polarization is defined as [15]:

$$\overrightarrow{P}_{f} = d_{3}(\operatorname{div}\widehat{c})\widehat{c} - d_{4}(\widehat{c}\cdot\operatorname{rot}\widehat{c})\widehat{p} + d_{6}(\widehat{k}\cdot\operatorname{rot}\widehat{c})\widehat{p} + d_{9}(\operatorname{div}\widehat{c})\widehat{k},$$

$$\tag{4}$$

where d_i are flexoelectric moduli. $\overrightarrow{P}_f(x, z)$ writes

$$\overrightarrow{P}_{f} \simeq -d_{3}\cos\phi_{0}\,\widehat{c}\,\varphi_{x} + \left[d_{4}\varphi_{z} + d_{6}\sin\phi_{0}\,\varphi_{x}\right]\widehat{p} - d_{9}\cos\phi_{0}\,\varphi_{x}\,\widehat{k},\tag{5}$$

turning out to be bidimensionally modulated as well, then creating an internal field $\vec{E}(x, z)$, characterized by the potential $\Psi(x, z)$:

$$\vec{E}(x,z) = -\text{grad }\Psi(x,z) = -[\Psi_x \,\hat{i} + \Psi_z \,\hat{k}],\tag{6}$$

being $|\Psi(x,z)| \ll P_s D_x$, where D_x is the cell thickness. In the local frame $[\hat{c}, \hat{k}, \hat{p}]$ the internal field $\vec{E}(x,z)$ is:

$$\vec{E} = E_c \,\hat{c} + E_z \,\hat{k} + E_p \,\hat{p} = \sin\phi_0 \,\Psi_x \,\hat{c} - \Psi_z \,\hat{k} - \cos\phi_0 \Psi_x \,\hat{p},\tag{7}$$

and couples with \overrightarrow{P}_{f} , giving

$$f_{flexo} = -\overrightarrow{P}_{f} \cdot \overrightarrow{E} =$$

$$= \frac{1}{2} (d_3 + d_6) \sin 2\phi_0 \varphi_x \Psi_x + d_4 \cos \phi_0 \varphi_z \Psi_x - d_9 \cos \phi_0 \varphi_x \Psi_z.$$
(8)

Dielectric term

The dielectric contribution to the cell free energy density writes

$$f_{diel} = -\frac{1}{8\pi} \overrightarrow{D} \cdot \overrightarrow{E}, \qquad (9)$$

where

$$\overrightarrow{D} = \overline{\overline{\varepsilon}} \, \overrightarrow{E} \,. \tag{10}$$

The rank 2 dielectric tensor $\overline{\overline{\varepsilon}}(\varepsilon_{\parallel}, \varepsilon_{p}, \varepsilon_{t})$ has only its diagonal components different from zero [16, 17], expressed in the intrinsic frame $[\hat{n}, \hat{p}, \hat{t}]$ where \hat{t} is the transverse unit vector $\hat{t} \equiv \hat{n} \times \hat{p}$. It takes into account the bonded charges separation in the chiral liquid crystal. Due to the fact that the wave amplitude $|\varphi|$ of the

periodic distortion is much smaller than ϕ_0 , the director \hat{n} reads

$$\hat{n} = -\sin\phi\sin\theta\,\hat{i} + \cos\phi\sin\theta\,\hat{j} + \cos\theta\,\hat{k} = \simeq -\sin\theta(\sin\phi_0 + \varphi\,\cos\phi_0)\,\hat{i} + +\sin\theta(\cos\phi_0 - \varphi\sin\phi_0)\,\hat{j} + \cos\theta\,\hat{k} .$$
(11)

Thus, from Eqs. (9 - 11) the free energy term is

$$f_{diel} = -\frac{\varepsilon_{\parallel}}{8\pi} (\overrightarrow{E} \cdot \widehat{n})^2 - \frac{\varepsilon_p}{8\pi} (\overrightarrow{E} \cdot \widehat{p})^2 - \frac{\varepsilon_t}{8\pi} (\overrightarrow{E} \cdot \widehat{t})^2 \quad (12)$$

and eventually becomes

$$f_{diel} = -\frac{\varepsilon_{\parallel}}{8\pi} (\sin\theta \sin\phi_0 \Psi_x - \cos\theta \Psi_z)^2 - \frac{\varepsilon_p}{8\pi} (\cos\phi_0 \Psi_x)^2 + -\frac{\varepsilon_t}{8\pi} (\cos\theta \sin\phi_0 \Psi_x + \sin\theta \Psi_z)^2.$$
(13)

Electrostatic interaction term among bonded charges The Coulomb interaction free energy density between spontaneous polarization charges Q, Q' separated at the same surface in correspondence of two smectic layers l, l' is given by

$$f_C = \pm \frac{1}{2} \frac{|Q||Q'|}{|\vec{r}' - \vec{r'}|} \frac{1}{V}$$
(14)

where V is the relevant volume, $\overrightarrow{r'}$, $\overrightarrow{r'}$ are the positions of Q, Q', and the sign to be chosen is either (+) or (-) respectively for ferroelectric- and antiferroelectric -phases, according to the fact that interacting dipole charges separated at the same cell surface are of the same or different signs. This means that a chiral LC in ferroelectric state has a repulsive coulombian potential, since the charges separated at the same surface in correspondence of adjacent layers have the same sign $(f_C = \alpha^2 Q^2/d)$, whereas in antiferroelectric state it has attractive coulombian potential, since the charges separated have alternatively opposite sign $(f_C = -\alpha^2 Q^2/d)$ - note that α is a convenient constant and d is the smectic layer thickness. More precisely f_C writes

$$f_C = \pm \frac{1}{2} \int \int \frac{\sigma \, dA \, \sigma' \, dA'}{|z' - z| D_x D_y D_z},\tag{15}$$

where σ , σ' are the surface charges densities at the walls, dA, dA' are the relevant surface elements and D_i is the cell size along the *i*-direction. Putting P_s , P'_s as the involved spontaneous polarizations, the corresponding charges are

$$\sigma \, dA = \overrightarrow{P}_s \cdot d\overrightarrow{A} = \overrightarrow{P}_s \cdot D_y \, dz \, \widehat{i}$$

$$\sigma' \, dA' = \overrightarrow{P}'_s \cdot d\overrightarrow{A} = \overrightarrow{P}'_s \cdot D_y \, dz' \, \widehat{i}.$$
(16)

Approximating Dirac delta function by $\delta(z) = 1/|z-z'|$, the integration of Eq. (15) over the whole cell gives

$$f_C = \pm \frac{1}{2} (\operatorname{div} \overrightarrow{P}'_s)^2 D_x D_y.$$
 (17)

The local spontaneous polarization is

$$\vec{P}_s = P_s \hat{p} = P_s [\cos \phi \, \hat{i} + \sin \phi \, \hat{j}] = \simeq P_s [(\cos \phi_0 - \varphi \sin \phi_0) \, \hat{i} + (\sin \phi_0 + \varphi \cos \phi_0) \, \hat{j}], \qquad (18)$$

and the divergence is

div
$$\overrightarrow{P}_s = \frac{\partial P_{sx}}{\partial x} \simeq -P_s \sin\phi_0 \varphi_x.$$
 (19)

The Coulomb term eventually reads

$$f_C = \pm \frac{1}{2} P_s^2 \sin^2 \phi_0 D_x D_y \varphi_x^2, \qquad (20)$$

where (+) and (-) are relevant to the ferroelectric- and antiferroelectric- states, respectively. The total bulk free energy density is the sum of all contributions already mentioned:

$$f = f_{el} + f_{flexo} + f_{diel} + f_C.$$

$$(21)$$

In the hypothesis that the anchoring is strong, the total free energy coincides with the total bulk free energy. By minimizing it with the usual procedure, the Euler-Lagrange Eqs.

$$\begin{cases} -\frac{\partial}{\partial z} \left(\frac{\partial f}{\partial \varphi_z} \right) - \frac{\partial}{\partial x} \left(\frac{\partial f}{\partial \varphi_x} \right) + \frac{\partial f}{\partial \varphi} = 0\\ -\frac{\partial}{\partial z} \left(\frac{\partial f}{\partial \Psi_z} \right) - \frac{\partial}{\partial x} \left(\frac{\partial f}{\partial \Psi_x} \right) + \frac{\partial f}{\partial \Psi} = 0 \end{cases}$$
(22)

can be written as

$$\begin{bmatrix}
B_1 \sin^2 \phi_0 + B_2 \cos^2 \phi_0 \pm \frac{1}{2} P_s^2 \sin^2 \phi_0 D_x D_y] \varphi_{xy} + \\
+ B_3 \varphi_{zz} - 2B_{13} \sin \phi_0 \varphi_{xz} + d \sin 2\phi_0 \Psi_{xx} + d^* \cos \phi_0 \Psi_{xz} = 0 \\
[\sin^2 \phi_0 (\varepsilon_{\parallel} \sin^2 \theta + \varepsilon_t \cos^2 \theta) + \varepsilon_p \cos^2 \phi_0] \Psi_{xx} + \\
+ (\varepsilon_{\parallel} \cos^2 \theta + \varepsilon_t \sin^2 \theta) \Psi_{zz} - (\varepsilon_{\parallel} - \varepsilon_t) \sin 2\theta \sin \phi_0 \Psi_{xz} + \\
- 2\pi d \sin 2\phi_0 \varphi_{xx} - 4\pi d^* \cos \phi_0 \varphi_{xz} = 0
\end{bmatrix}$$
(23)

where $d \equiv (d_3 + d_6)/2$, $d^* \equiv d_4 - d_9$ are combinations of the flexoelectric moduli. System (23) is comprising two 2^{nd} order linear differential equations in the azimuth $\varphi(x, z)$ and the internal electric potential $\Psi(x, z)$. The system admits harmonic solutions as the following:

$$\begin{pmatrix} \varphi \\ \Psi \end{pmatrix} = \begin{pmatrix} \varphi_{max} \\ \Psi_{max} \end{pmatrix} \exp[i(q_x x + q_z z)], \qquad (24)$$

where q_x , q_z represent the wave-vector of the possible biperiodic coupled distortion. By substituting Eq. (24) into linearized Euler- Lagrange Eqs. (23), a linear system in $\varphi(x, z)$, $\Psi(x, z)$ is obtained. The nontriviality condition yields to the dispersion relation

$$[B_{3}r^{2} - 2B_{13}\sin\phi_{0}r + B_{2}\cos^{2}\phi_{0} + B_{1}\sin^{2}\phi_{0} \pm \frac{1}{2}P_{s}^{2}\sin\phi_{0}D_{x}D_{y}] + \frac{4\pi[\frac{1}{2}d\sin2\phi_{0} + d^{*}\cos\phi_{0}r]^{2}}{\sin\phi_{0}(\varepsilon_{\parallel}\sin^{2}\theta + \varepsilon_{t}\cos^{2}\theta) - (\varepsilon_{\parallel} - \varepsilon_{t})\sin2\theta r + (\varepsilon_{\parallel}\cos^{2}\theta + \varepsilon_{t}\sin^{2}\theta)r^{2}} = 0$$
(25)

where the wave-vector ratio is defined as

$$r \equiv q_z/q_x. \tag{26}$$

The minimum value of r, which satisfies the condition (25), determines the threshold of the appearance of the biperiodic instability. In the case of strong anchoring, it turns out to be

$$q_x = \frac{\pi}{D_x} \simeq 1 \mu m^{-1}, \tag{27}$$

since at the cell walls the director is kept in its undeformed position: $\varphi(x = 0, z) = 0$, $\varphi(x = D_x, z) = 0$, and the minimum energy distortion has the wavelength λ_x equal to the double cell thickness, $\lambda_x = 2D_x$, where $D_x \approx 2 \ \mu$ m.

If the elastic constants for bend B_1 and for splay B_2 are equal and if the dielectric permittivity is isotropic, $\varepsilon_{\parallel} = \varepsilon_p = \varepsilon_t \equiv \varepsilon$, the dispersion relation can be written more simply as

$$B_3 r^2 - B_{13} \sin\phi_0 r + B_2 \pm P_s^2 \sin\phi_0 D_x D_y + 4\pi \frac{[d\sin 2\phi_0 + d^* \cos\phi_0 r]^2}{\varepsilon[\sin\phi_0 + r^2]} = 0,$$
(28)

resulting in a 4^{th} degree algebraic equation. Let us remind the correspondence between the smectic C^{*} and the nematic elastic constants

$$\begin{cases}
B_{1} = \frac{1}{4}K_{22}\sin^{2}2\theta + K_{33}\sin^{4}\theta, \\
B_{2} = K_{11}\sin^{2}\theta, \\
B_{3} = K_{22}\sin^{4}\theta + \frac{1}{4}K_{33}\sin^{2}2\theta, \\
B_{13} = \frac{1}{2}(K_{33} - K_{22})\sin2\theta\sin^{2}\theta,
\end{cases}$$
(29)

where the smectic tilt $\theta = \theta(T)$ is only dependent on temperature T. At room temperature $T = 25^{\circ}C$ it has the typical value $\theta \sim 20^{\circ}$. The usual values of the other relevant parameters are $B_1 \sim B_2 \sim B_3 \sim 0.1 \div 0.5$, $K_{ii} \sim 10^{-6}$ dyn, $B_{13} \sim \pm B_1 \sim \pm 10^{-6}$ dyn, $d \sim 10^{-5}$ dyn, $d^* \sim \pm 10^{-5}$ dyn, $P_s \sim (0.05 \div 50)$ nC/cm², $\phi_0 \sim 10^{\circ} \div 90^{\circ}$, $\varepsilon = 1$. Hence the last term of Eq. (28) turns out to be negligible. If the elastic coupling no commar bend-twist, B_{13} is negligible (for rigid smectic planes, $B_{13} = 0$) and if the splay does not influence the phenomenon ($B_2 = 0$), thus (28) reduces to

$$B_3 r^2 \pm \frac{1}{2} P_s^2 \sin \phi_0 D_x D_y \simeq 0, \qquad (30)$$

giving simply:

$$r^2 = \mp \frac{D_x D_y}{2B_3} \sin\phi_0 P_s^2. \tag{31}$$

We point out that only in *antiferroelectric state* this model predicts the existence of the biperiodic distortion for smectic C^* cells in bookshelf geometry with strong



Figure 3. Ratio $r = \lambda_x/\lambda_z$ between the wavelengths of the two distortion modes characterizing the biperiodic instability as a function of the spontaneous polarization P_S . (a) The configuration are described by the pre-azimuth $\Phi_0 = 90^\circ - \Phi^*$ with $\Phi^* = 5^\circ \cdot 15^\circ$ (around maximum pre-tilt), and with $\Phi_0 = \Phi^*$ (around unidirectional planarity). (b) Zoom of the same diagram around the threshold, showing that in the first case the transition is 2nd order, whereas in the second case it is 1storder.



Figure 4. The same as in Fig. 3, but (a) with $\Phi^* = 25^{\circ} \cdot 45^{\circ}$. (b) Zoom of the same diagram around the threshold. When $\Phi_0 \ge 45^{\circ}$ the transition is 2nd order.

anchoring. Then in the case of elastic- and dielectricisotropy, by neglecting the flexoelectrical corrections, the wave-vector ratio turns out to be proportional to the spontaneous polarization of one smectic plane:

$$r = \beta P_s, \tag{32}$$

where

$$\beta = \sqrt{\frac{D_x D_y}{2B_3}} \sin\phi_0. \tag{33}$$

In a more general case Eq. (28) holds and it is necessary to perform a numerical calculation. As a result, in Figs. 3a and 4a the wave-vector ratio as a function of the spontaneous polarization is reported for different values of pre-azimuth Φ_0 . When $\Phi_0 = 0^\circ$, in the initial conditions the tilt director \hat{c} is normal to the cell plates; when $\Phi_0 = 90^\circ$, the tilt director \hat{c} lies in the cell plates, and the \hat{n} -orientation is unidirectional planar. According to the present model, numerical calculations performed on the dispersion relation Eq. (28) demonstrate that the biperiodic pattern is a threshold phenomenon, with the wavelength λ_x bonded to the cell thickness in the case of strong anchoring. Above the threshold, the wavelength λ_z is almost inversely proportional to the smectic layer spontaneous polarization ${\cal P}_s$, and increases with the pre-azimuth as well. In Fig. 3b and 4b a zoom of the origin zone of Fig. 3a and 4a is reported, showing that for pre-azimuth $\Phi_0 \sim 0^\circ$, implying pre-tilt close to the smectic tilt θ , the transition is of the first order, whereas for pre-azimuth $\Phi_0 \sim 90^\circ$, implying a quasi-planar configuration, the transition is of the second order. The first order character yields in the range $\Phi_0 = 0^{\circ} - 45^{\circ}$, whereas the second order character yields in the range $\Phi_0 = 45^{\circ}-90^{\circ}$. In any case the P_s -threshold diminishes as the pre-azimuth Φ_0 increases as well, converging to a minimum critical value ≈ 0.2 ues.

III Conclusions

The arising of periodical instability in smectic C^* has been analysed and a new model in the frame of continuum theory has been established. According to our model, a soft mixed bend- and twist- distortion spontaneously arises in homogeneous surface stabilised cells ordered in bookshelf geometry, when the external field is switched off. Such distortion is biperiodical, since the two wave-vectors instead of wave vector and directions instead of direction. In antiferroelectric configuration it can be explained without invoking smectic planes- and layers deformation, as a competition between the coupling of spontaneous polarisation-internal electric field and the Coulombian interaction among charges separated in smectic layers at the cell walls. Such competition is driven by anchoring and is mediated by elasticity. The dielectric- and flexoelectric- contributions just give small corrections to this picture. In the case of strong

anchoring, the wave-vector ratio is proportional to the spontaneous polarisation of one smectic plane. However, in the ferroelectric state, such type of biperiodical distortion is hindered.

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References

- R.B. Meyer, L. Liebert, L. Strzelecki, and P. Keller, J. Phys (France) 36, L69 (1975).
- [2] N.A. Clark and S.T. Lagerwall, Appl. Phys. Lett. 36, 899 (1980).
- S.T. Lagerwall, Ferroelectric and Antiferroelectric Liquid Crystals, (Wiley-VCH, Weinheim, 1999).
- [4] Yu.P. Panarin, E.P. Pozhidaev, and M.I. Barnik, Mol. Mat. 1, 29 (1992).
- [5] Tadashi Akahane and Atsushi Obinata, Liq. Cryst. 15, 883 (1993) et ref. therein.
- [6] L.A. Beresnev, M.V. Loseva, N.I. Chernova, S.G. Kononov, P.V. Adomenas, and E.P. Pozhidaev, Pisma JETF, 51, 457 (1990).
- [7] L.A. Beresnev, M. Pfelffer, W. Haase, N.I. Chernova, and P.V. Adomenas, Pisma JETF, 53, 170 (1991).
- [8] L. Lejcek and S. Pirkl, Liq. Cryst. 8, 871 (1990).
- [9] J. Pavel and M. Glogarova, Liq. Cryst. 9, 87 (1991).
- [10] R.F. Shao, P.C. Willis, and N.A. Clark, Ferroelectrics 121, 127 (1991).
- [11] V.P. Vorflusev, Yu.P. Panarin, S.A. Pikin, and V.G. Chigrinov, (unpublished).
- [12] J. MacLennan, Europhys. Lett. 13, 435 (1990).
- [13] S.A. Pikin, Mol. Cryst. Liq. Cryst. 215, 73 (1992).
- [14] F.M. Leslie, I.W. Stewart, and M. Nakagawa, Mol. Cryst. Liq. Cryst. 198, 443 (1991).
- [15] I. Dahl, Ferroelectrics 84, 345 (1988).
- [16] C.J. Elston, J.R. Sambles, and M.G. Clark, J. Appl. Phys. 68, 1242 (1990).
- [17] J.C. Jones, E.P. Raynes, M.J. Towler, and J.R. Sambles, Mol. Cryst. Liq. Cryst. 199, 277 (1991).