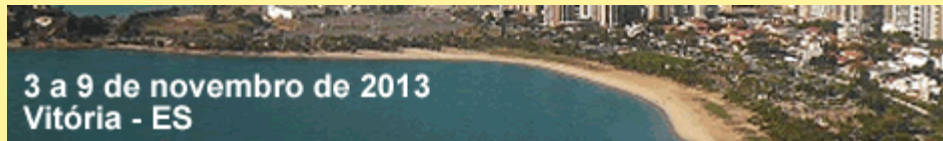


# Magnetic vortices, skyrmions, etc.

Alberto P. Guimarães,  
Centro Brasileiro de Pesquisas Físicas (CBPF),  
Rio de Janeiro, Brazil

**IX Escola Brasileira de Magnetismo**



08/11/2013

# Collaborators

Dr. F. Garcia (CBPF), Brazil

Dr. J.P. Sinnecker (CBPF), Brazil

E.R.P. Novais (CBPF), Brazil

H.V.Cotrina (CBPF), Brazil

G.B.M. Fior (LNLS), Brazil

# Outline

1. Solitons and magnetic vortices
2. Topological properties of vortices, etc
3. Formation of a skyrmion

# Solitons

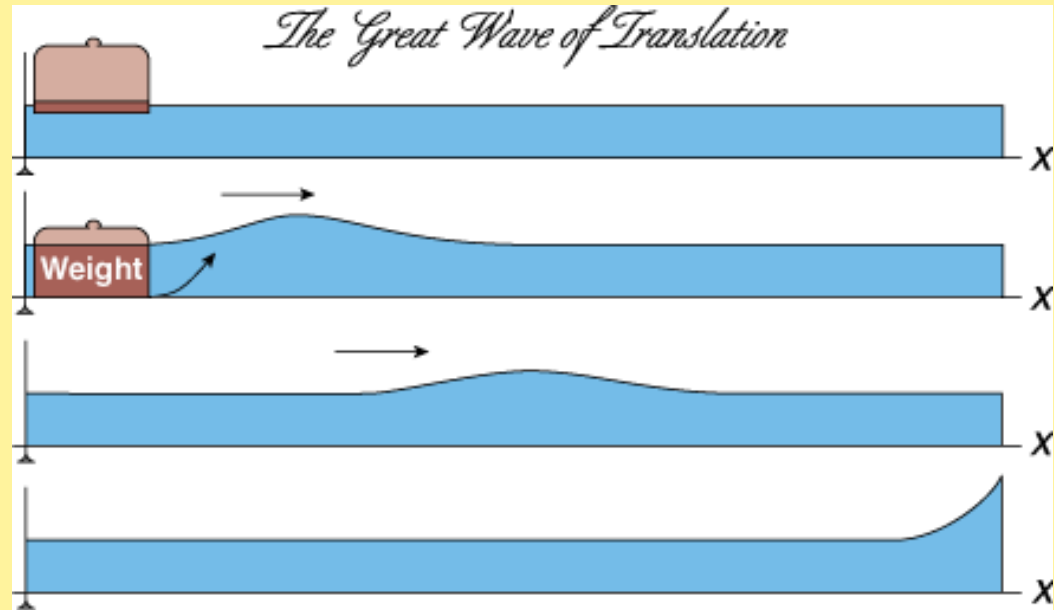
Waves in a narrow channel travel long distances without changing their shape

J. S. Russell, Report of the Fourteenth Meeting of the British Association for the Advancement of Science (Murray, London, 1844), pp. 311-390.

John Scott Russell (1808–1882)

Solitons are collective excitations that are solutions of differential equations

Topological solitons (or topological defects): those whose stability is guaranteed topologically

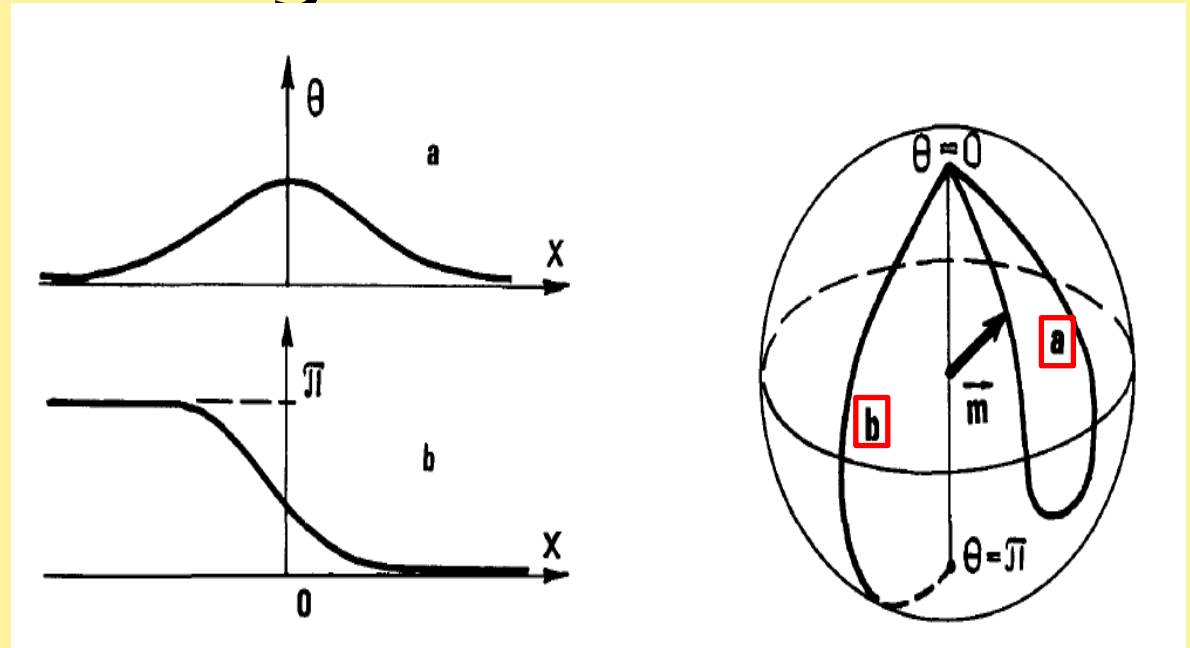


# Examples of solitons



<http://www.youtube.com/watch?v=Ud7STKWNmQw>

# Solitons in a one-dimensional magnet



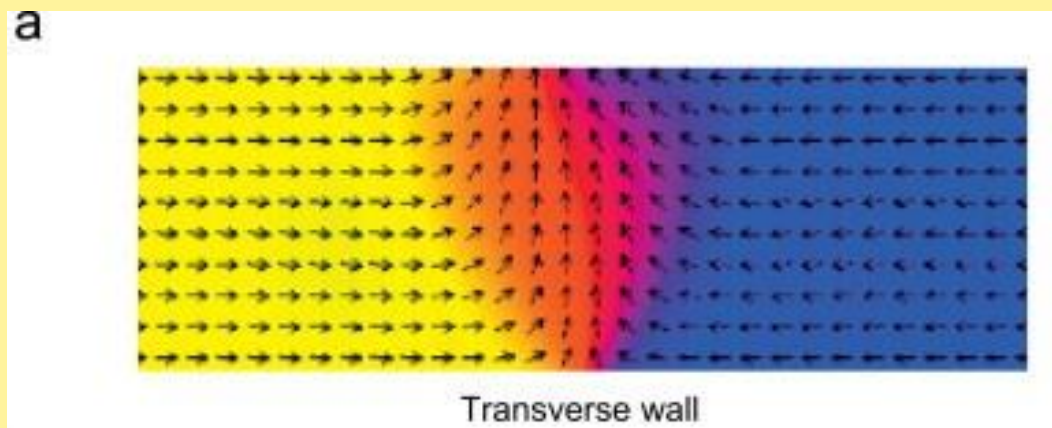
- a) Dynamic soliton: topologically unstable, since curve a on the sphere can be deformed continuously to a point (the ground state)(these configurations are said to be topologically equivalent)
- b) Topological soliton: curve b cannot be deformed to a point

# Real systems

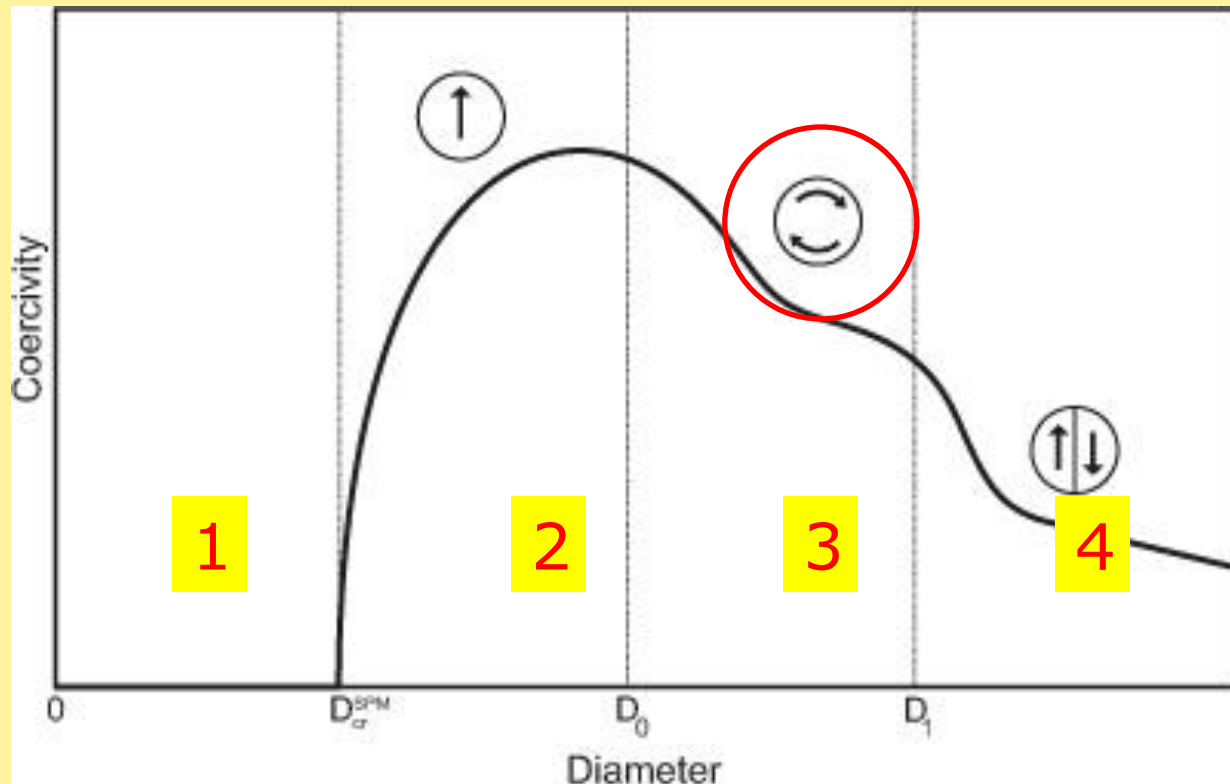
Two configurations are topologically equivalent when they can be transformed into one another without overcoming an infinite energy barrier

Considerations:

- a) In real systems, the energy barriers are not infinite;
- b) Real systems have finite dimensions, therefore, e.g., one can always expel a domain wall from a sample



# Spin structures in nanoobjects



Four regimes:

1) superparamagnetic;

2) single-domain FM;

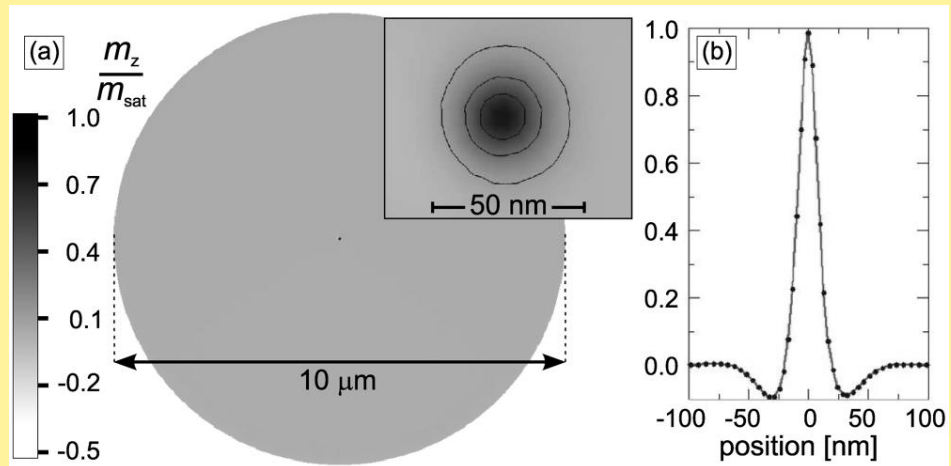
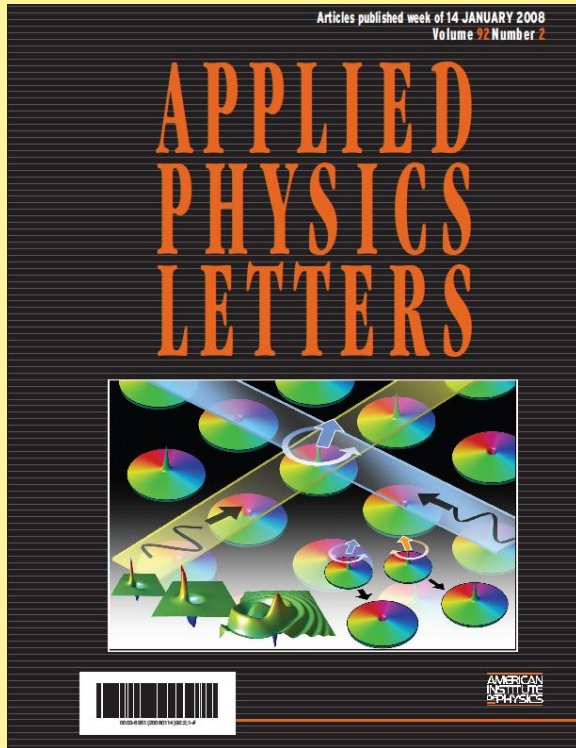
3) vortex state;

4) multidomain FM

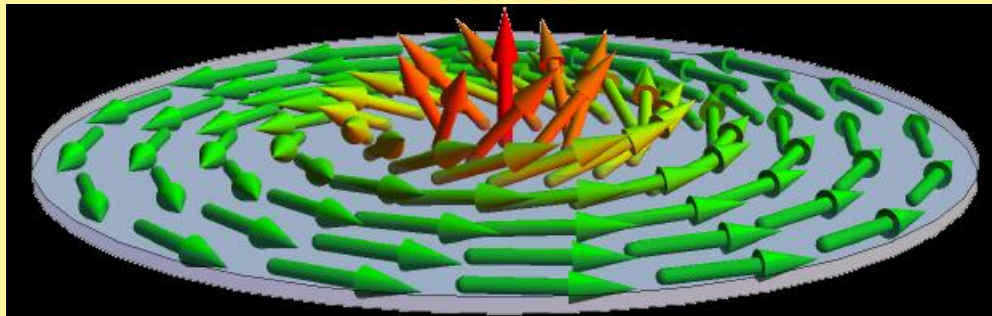
Schematic curve of coercivity vs. diameter for soft magnetic particles.



# Properties of magnetic vortices



Computed vortex and core profile Bode, PRL 100, 029703 (2008)



Pigeau

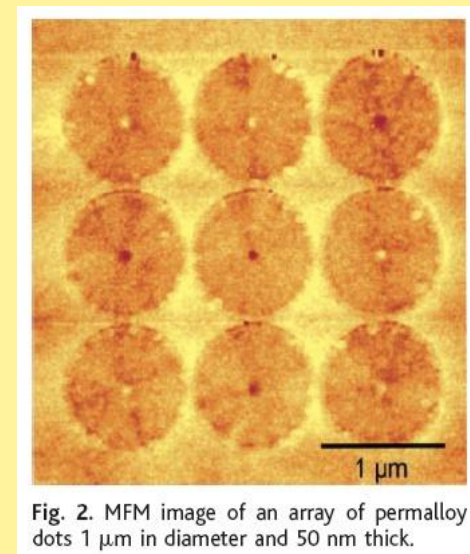
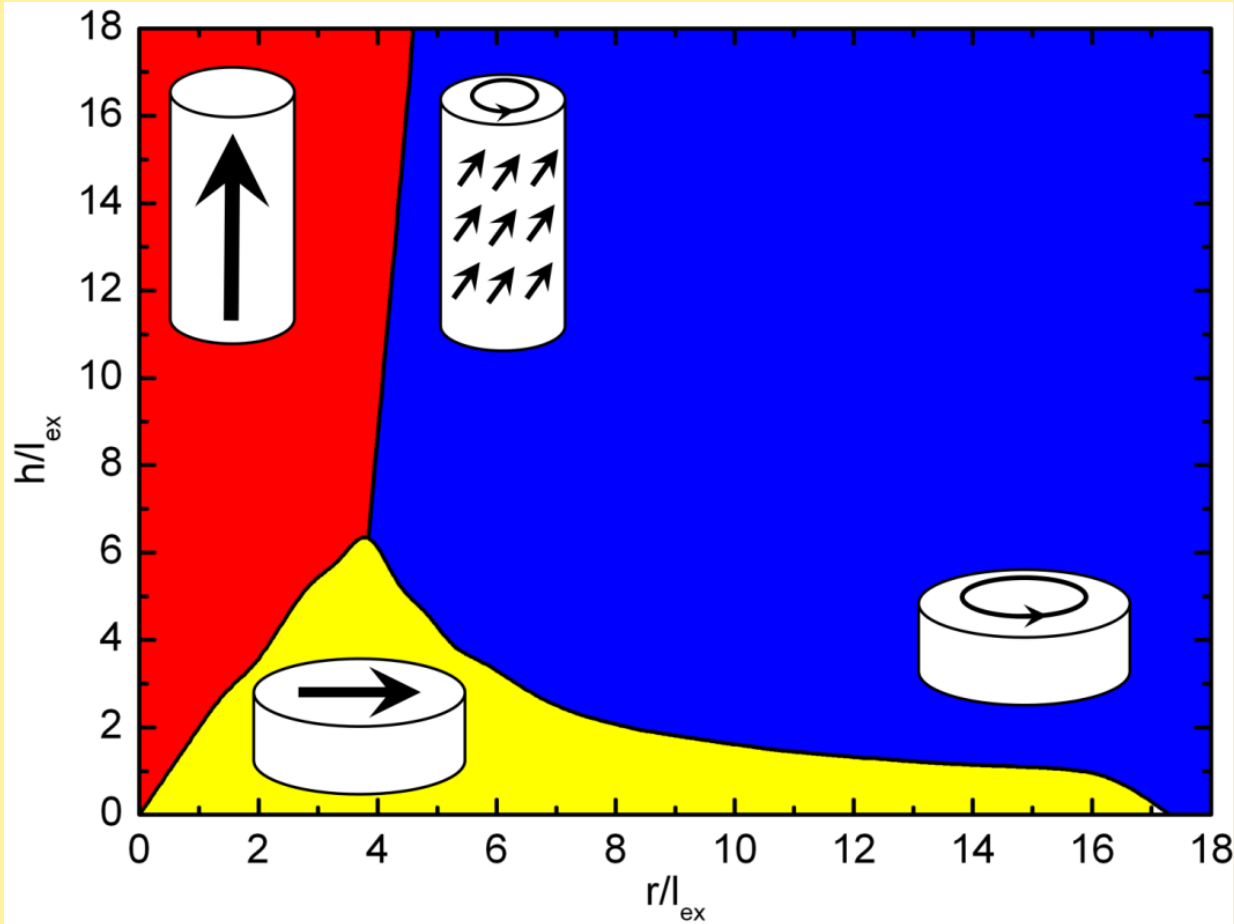


Fig. 2. MFM image of an array of permalloy dots 1  $\mu\text{m}$  in diameter and 50 nm thick.

Shinjo et al., Science 289, 930 (2000)

# Circular nanodots: phase diagram



Different spin configurations

Graph:  
Height vs. thickness

# Micromagnetic simulations

The properties of nanoscopic or microscopic magnetic samples may be simulated numerically. In the Micromagnetism approach, the magnetic medium is treated as a continuum.

The total energy is a sum of the terms of exchange, anisotropy, magnetostatic and Zeeman:

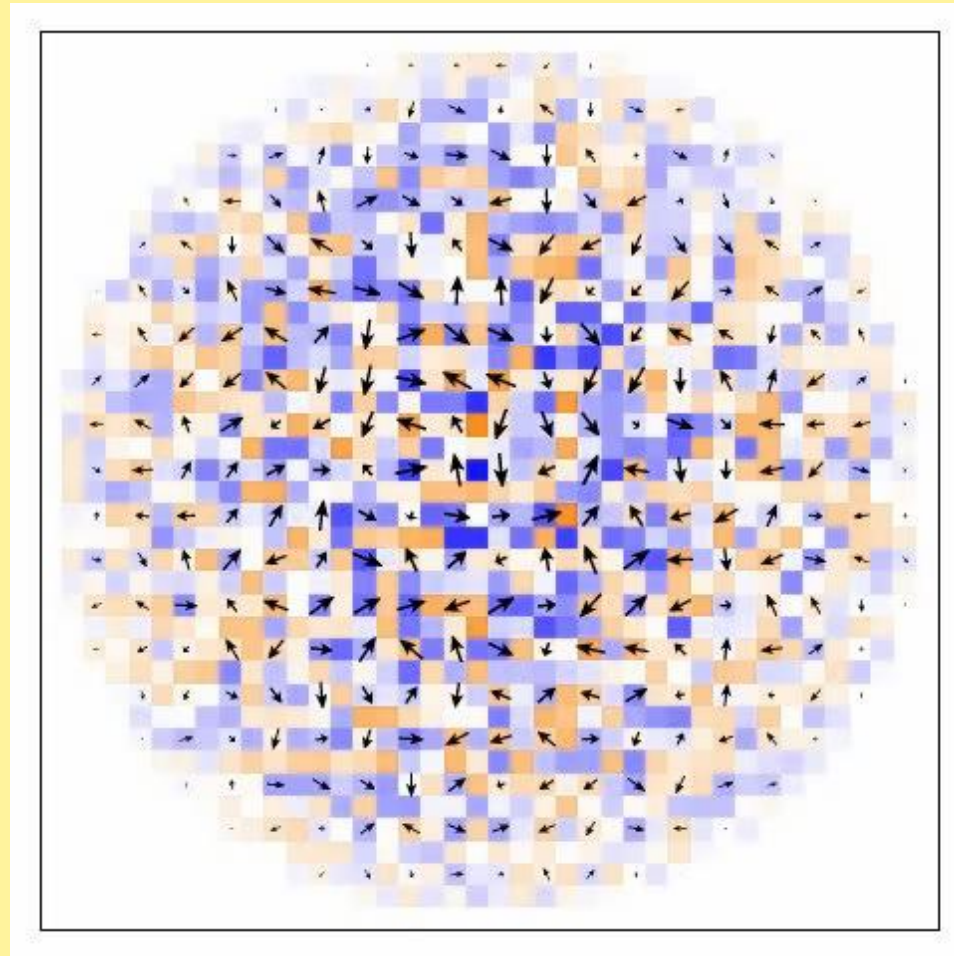
$$E_{\text{tot}} = E_{\text{ex}} + E_A + E_{\text{ms}} + E_{\text{ext}}$$

or

$$E = \int_V \left\{ A \left[ \nabla \left( \frac{\mathbf{M}}{M_s} \right) \right]^2 + K_1 \sin^2(\theta) - \frac{\mu_0}{2} \mathbf{M} \cdot \mathbf{H}_d(M) - \mu_0 \mathbf{M} \cdot \mathbf{H} \right\} dV$$

The spin configuration is found by minimizing the total energy  $E_{\text{tot}}$

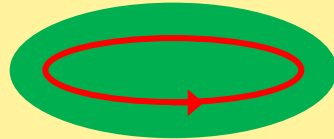
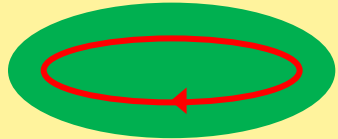
# Formation of a vortex on a permalloy nanodisk



# Properties of magnetic vortices

- Circulation:

$c = +1$  (CCW)    $c = -1$  (CW)



Combining  $c$  and  $p$ :

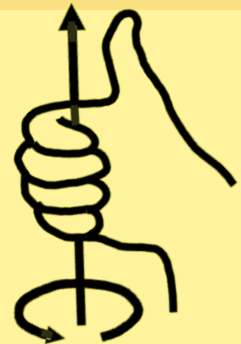
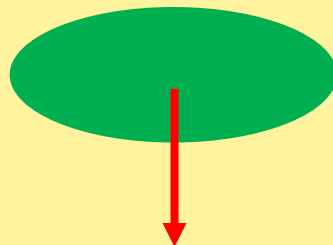
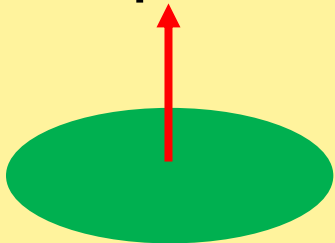
chirality or handedness:

$cp = \pm 1$

- Polarity:

$p = +1$

$p = -1$



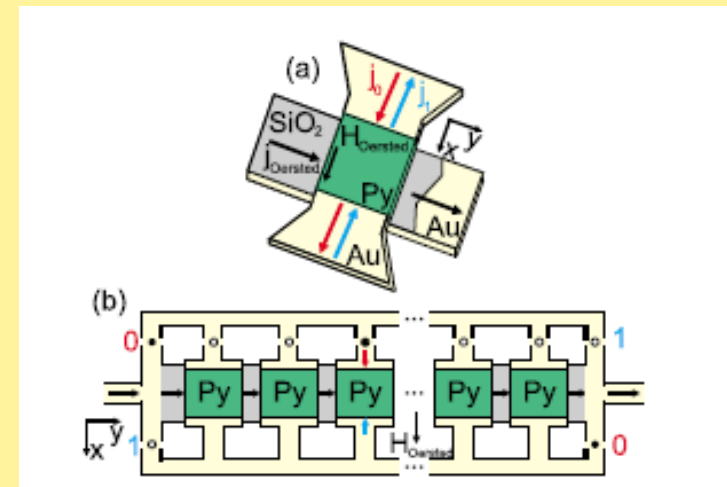
# a. Applications of vortex systems: Vortex Random-access Memory (VRAM)

Vortices may store 1 bit using

- a) Polarity
- b) Circulation (CW or CCW)
- c) Chirality

Or else store 2 bits using, e.g.,

- a) Polarity and circulation

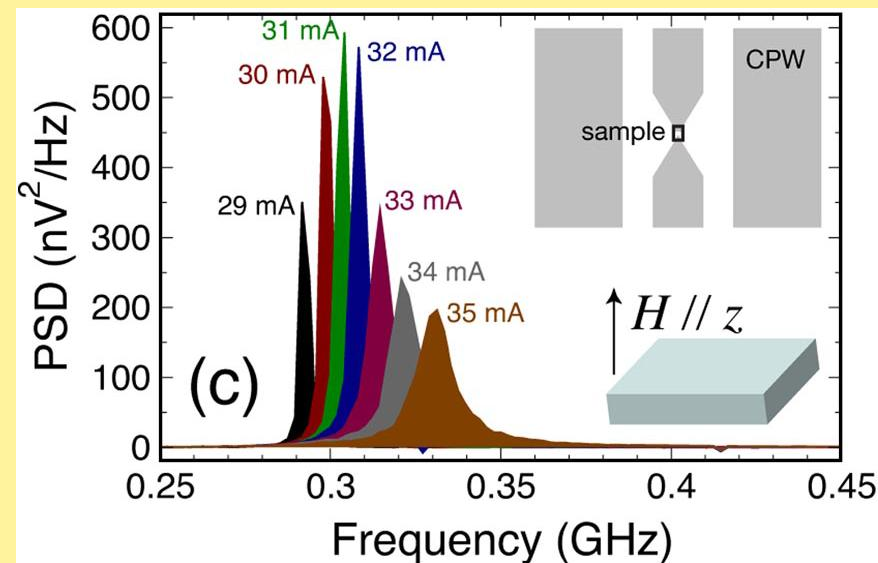


## b. Applications of vortex systems : spin torque nano-oscillators (STNOs)

Polarized spin currents can induce periodic motion of vortex cores (gyrotropic motion), also emitting RF

(Pufall 2007, Mistral 2008)

Coupling of vortices in spin valve nanopillar may increase rf power



# c. Applications of vortex systems : destruction of cancer cells

nature  
materials

ARTICLES

PUBLISHED ONLINE: 29 NOVEMBER 2009 | DOI: 10.1038/NMAT2591

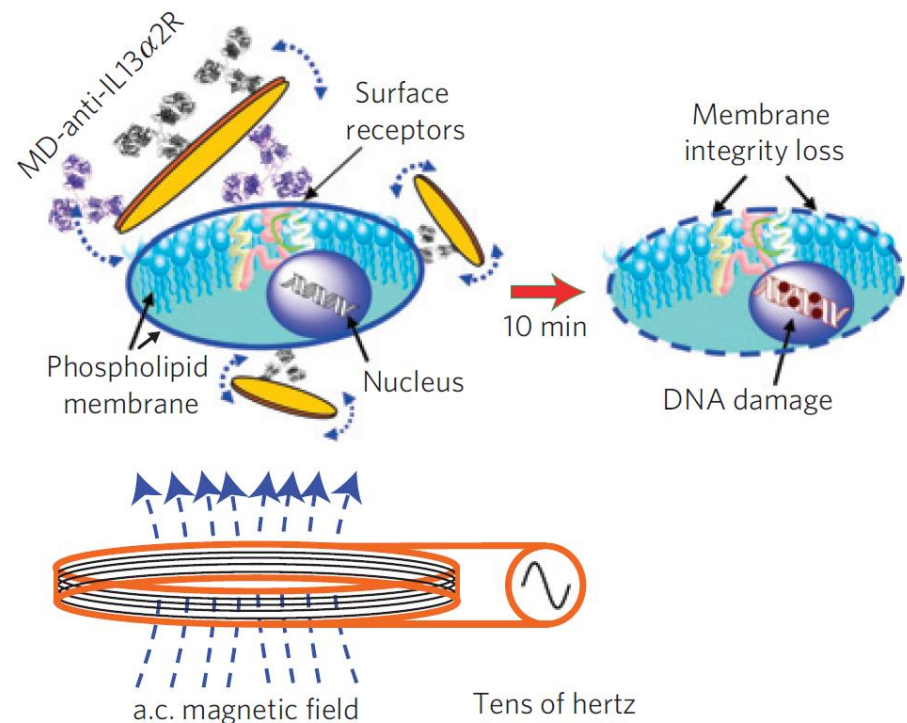
## Biofunctionalized magnetic-vortex microdiscs for targeted cancer-cell destruction

Dong-Hyun Kim<sup>1</sup>, Elena A. Rozhkova<sup>2\*</sup>, Ilya V. Ulasov<sup>3</sup>, Samuel D. Bader<sup>1,2</sup>, Tijana Rajh<sup>2</sup>,  
Maciej S. Lesniak<sup>3</sup> and Valentyn Novosad<sup>1\*</sup>

Torque  $\tau = \mathbf{m} \times \mathbf{H}$

Oscillation of the disks  
induces programmed cell  
death

Kim, Nature Mater. 9 165, (2010)

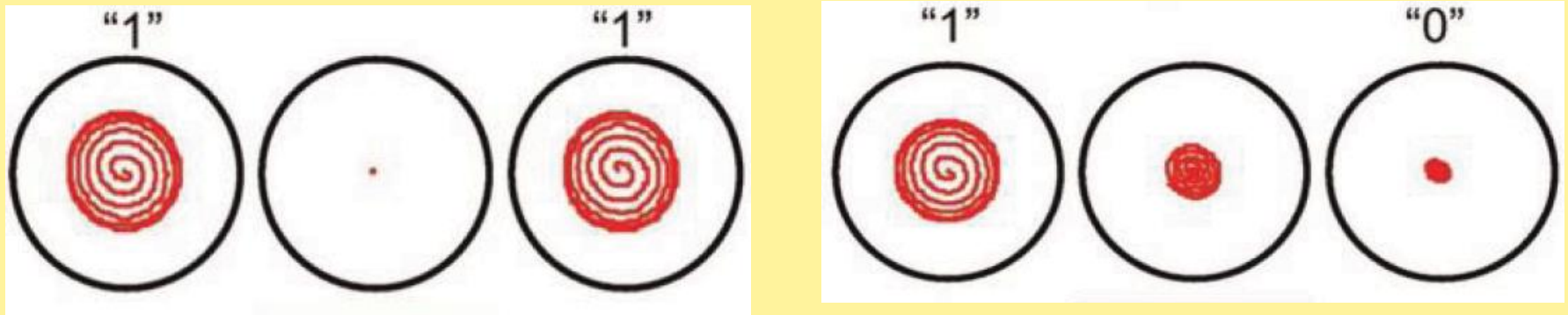




# d. Applications of vortex systems: logic gates

## Logic Operations Based on Magnetic-Vortex-State Networks

Hyunsung Jung,<sup>†</sup> Youn-Seok Choi,<sup>†</sup> Ki-Suk Lee,<sup>†</sup> Dong-Soo Han,<sup>†</sup> Young-Sang Yu,<sup>†</sup> Mi-Young Im,<sup>‡</sup> Peter Fischer,<sup>‡</sup> and Sang-Koog Kim<sup>†,\*</sup>

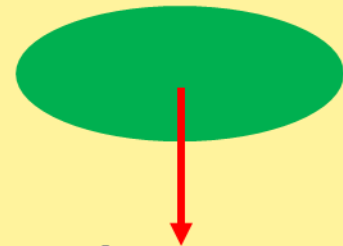
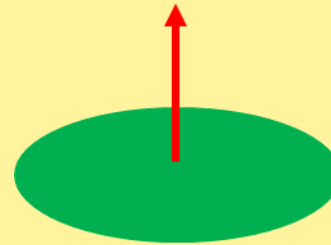


The output of the center disk is controlled by the input to disks 1 and 3

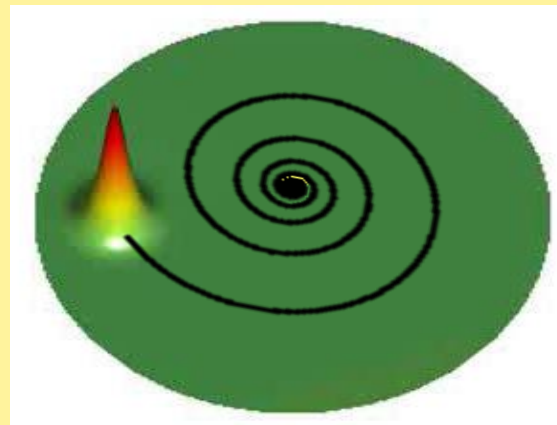
# Gyrotropic motion of vortex cores

The vortex core performs a spiral-like motion with a frequency related to the disk aspect ratio  $\beta=h/R$

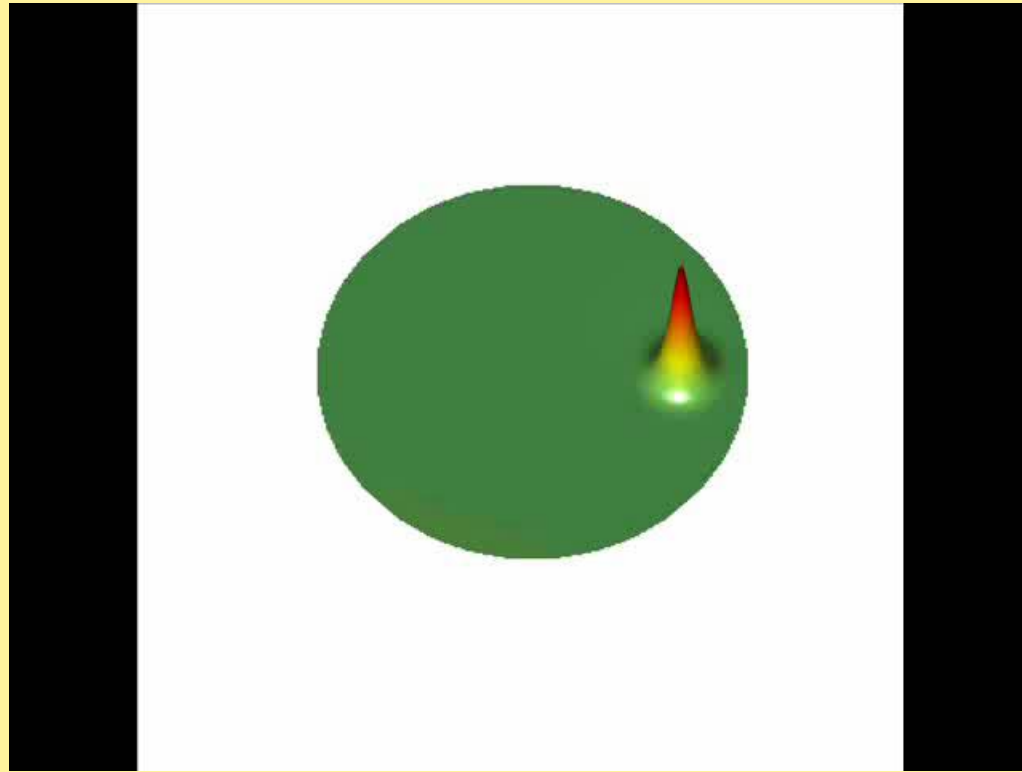
The direction of the translation is defined by the polarity  $p$  (up or down)



6



# Gyrotropic motion of a vortex core



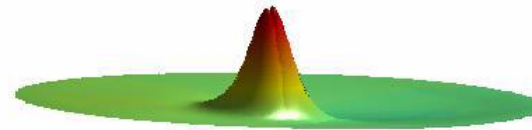
Translation motion of magnetic vortex core displaced from the equilibrium position (zero damping)

## Magnetic vortex echoes

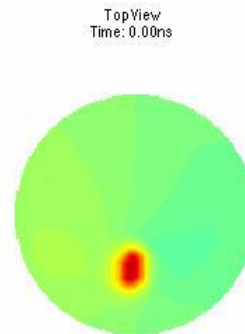
F. Garcia,<sup>1</sup> J. P. Sinnecker,<sup>2</sup> E. R. P. Novais,<sup>2</sup> and A. P. Guimarães<sup>2,a)</sup>

The vortex core motion of a inhomogeneous assembly of nanodisks produces an echo that may be used to characterize it

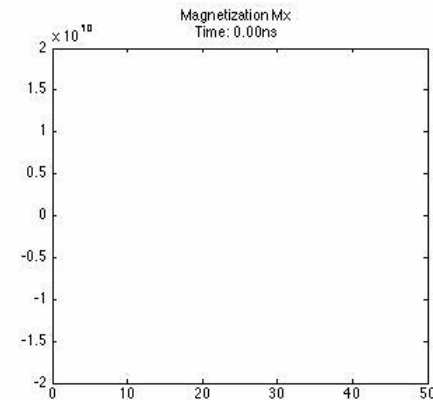
This is analogous to the NMR spin echo



Superposed image of several disks

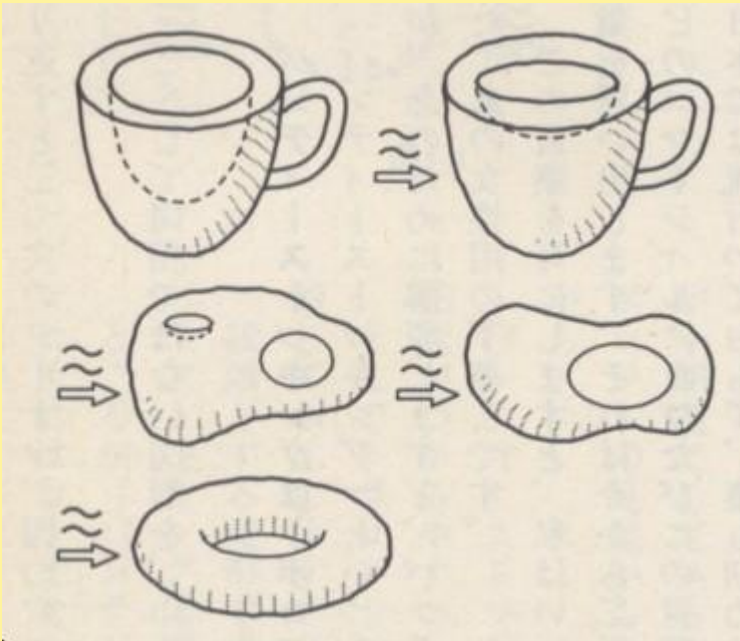


Projection of the image of the disks



The evolution of the total magnetization

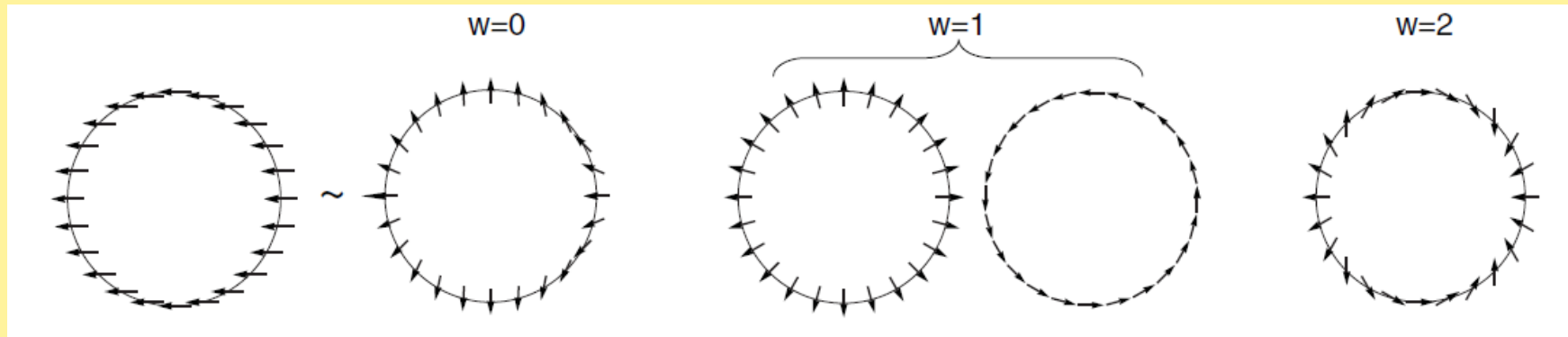
# Topology?!



[Jwilson.coe.uga.edu](http://Jwilson.coe.uga.edu)

Remember: in topological terms, one coffee cup=one donut

# Winding number

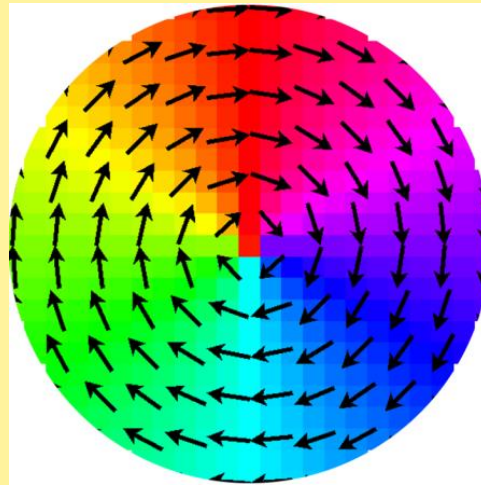


The winding number is the total variation of the magnetization angle  $\Delta\varphi$  as one moves counterclockwise around a circle, divided by  $2\pi$

One cannot deform a given spin configuration into another of different winding number

A topological defect exists if one cannot deform a spin configuration into the ferromagnetic state

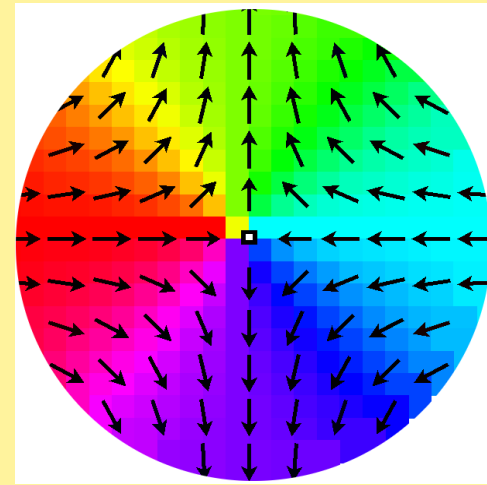
# Vortices and antivortices



Vortex

$$n=1$$

$$p=\pm 1$$



Antivortex

$$n=-1$$

$$p=\pm 1$$

When a vortex and an antivortex meet, they annihilate.

# Winding number $n$ and skyrmion number $q$

The winding number: total variation of the magnetization angle  $\Delta\varphi$  as one moves counterclockwise around a circle divided by  $2\pi$

$$n = \Delta\varphi / 2\pi$$

The winding number of a vortex is 1

The skyrmion number  $q$  is

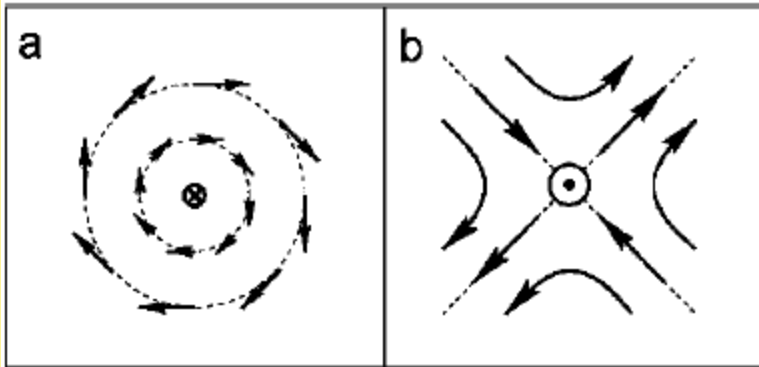
$$q = np/2$$

where  $p$  is the polarity



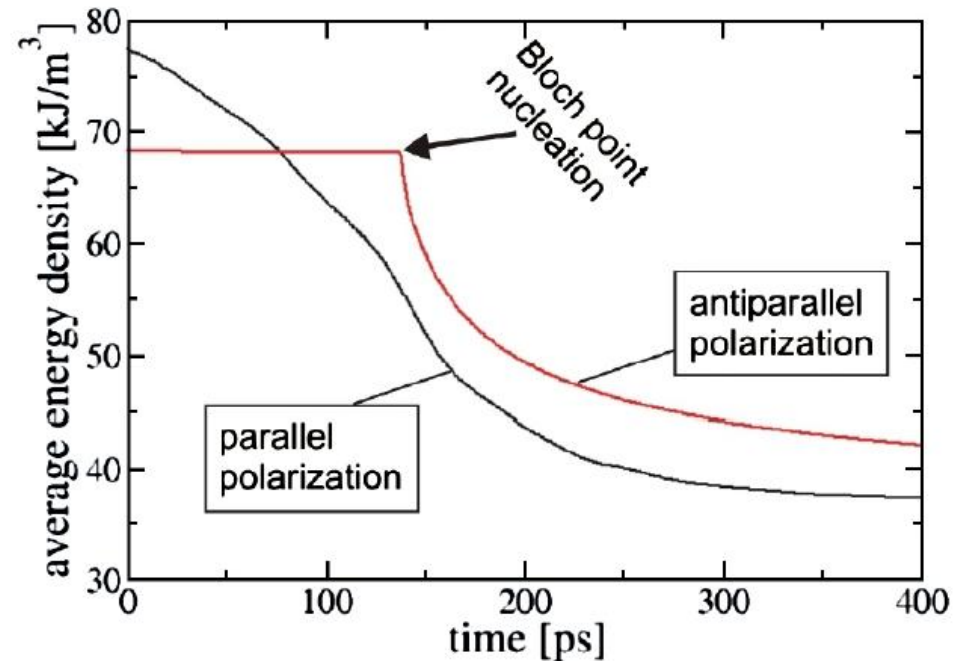
## Exchange Explosions: Magnetization Dynamics during Vortex-Antivortex Annihilation

Riccardo Hertel and Claus M. Schneider



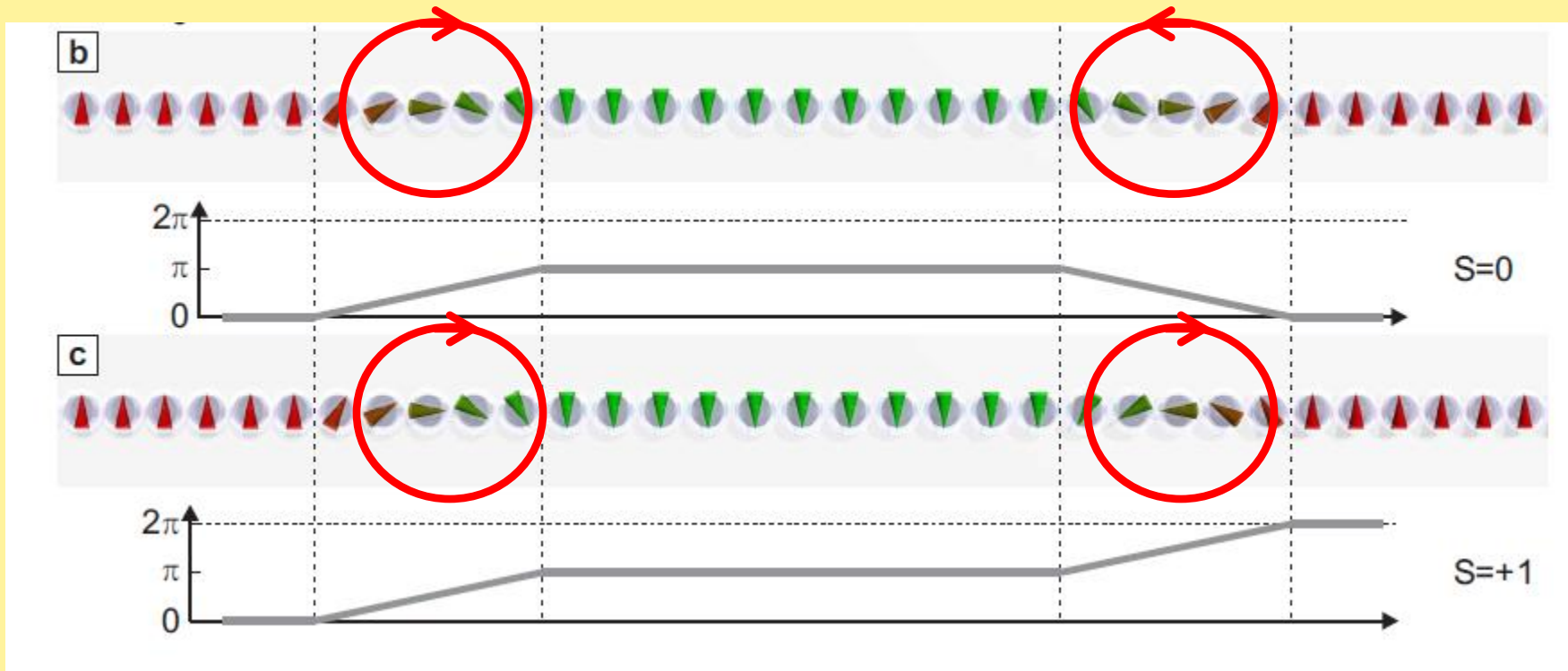
Vortex and antivortex

When the sum of the skyrmion numbers of the vortex and the antivortex is not zero, the annihilation releases a burst of energy



Annihilation of a vortex and the conservation of the skyrmion number

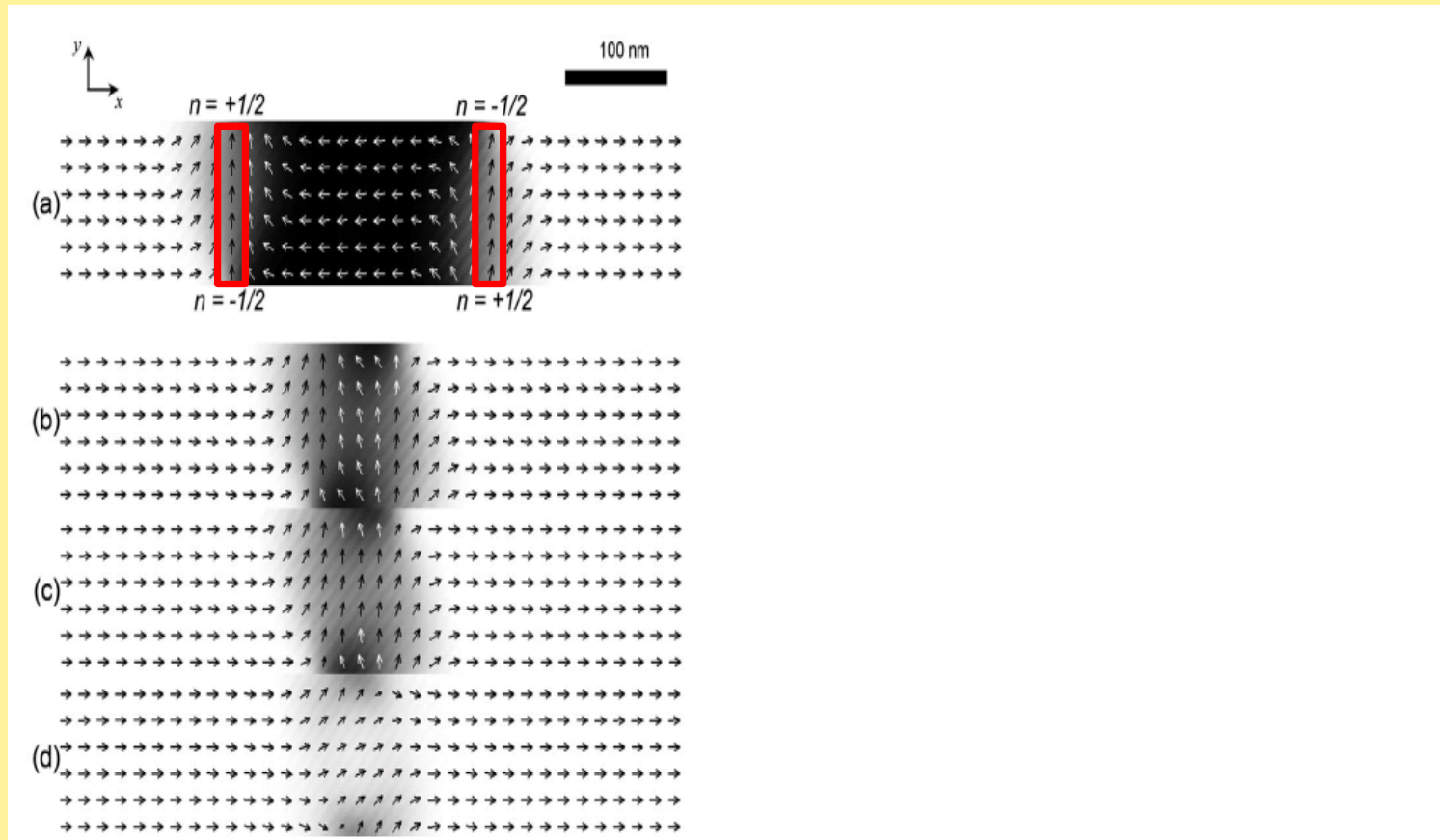
# 1D Domain walls and skyrmions



The importance of the winding number (and the total skyrmion number  $S$ )  
In b) the total skyrmion number  $S$  is zero  
In c)  $S=1$  and the one-dimensional domain walls need a higher field to be annihilated – a skyrmion is formed

# 2D Domain walls

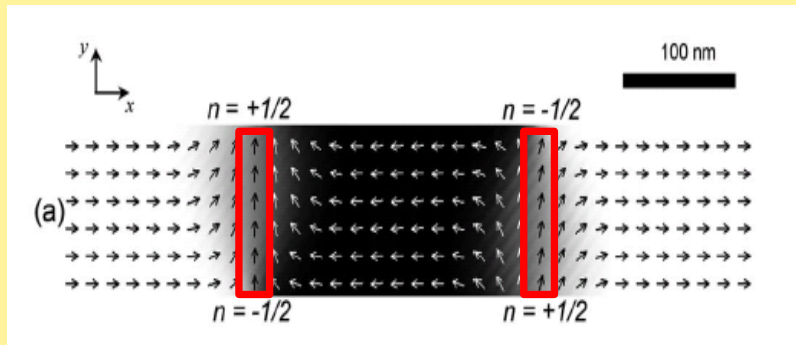
1)



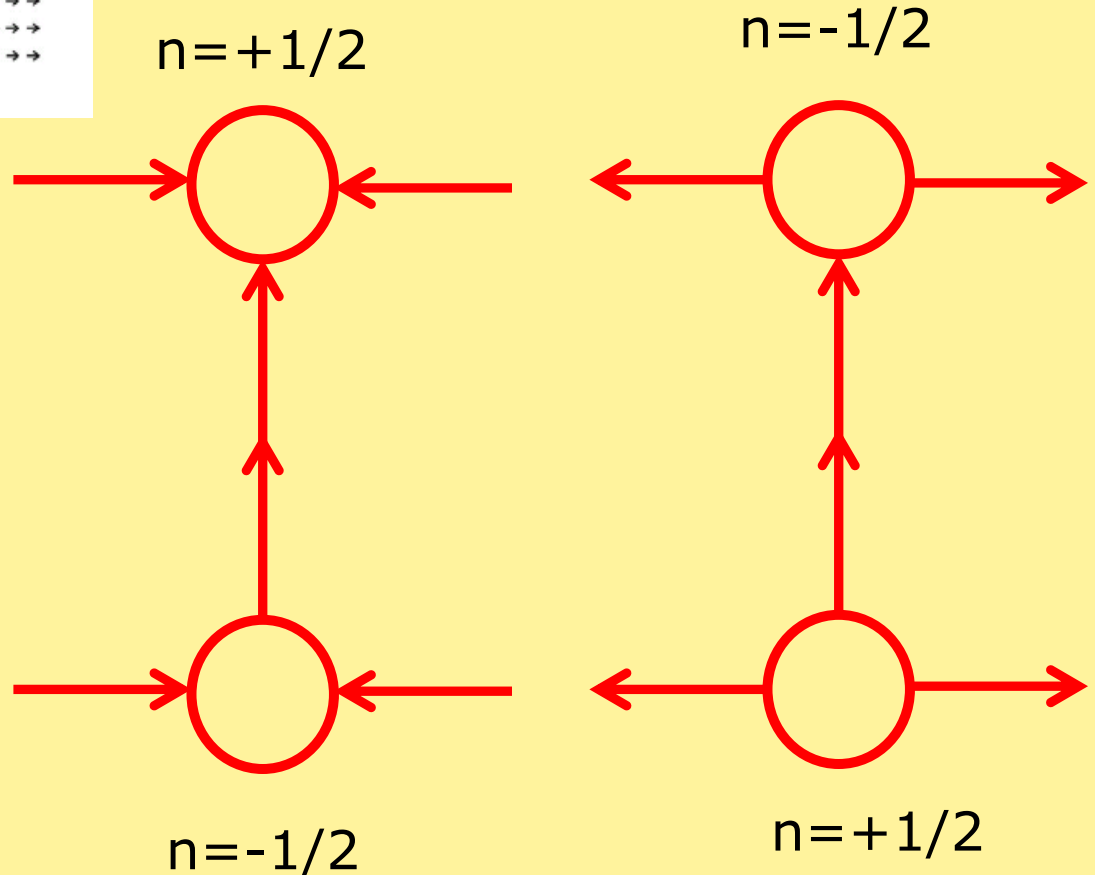
2)

Effect of applied field on domain walls with different topologies: 1)  $\Sigma q = 0$ , the walls disappear; 2)  $\Sigma q \neq 0$  topologically protected

# Edge defects in a domain wall



I



This is a representation of the first stripe (previous slide)

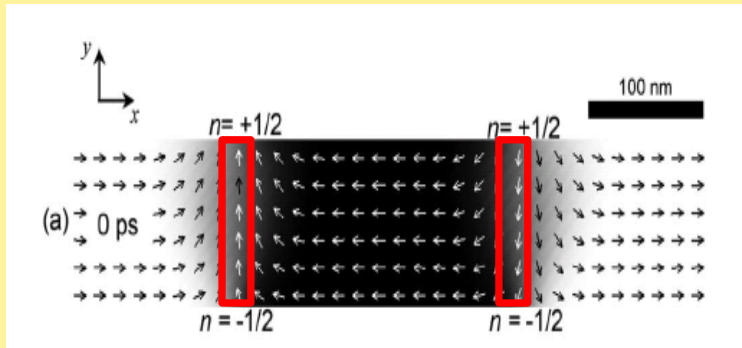
A DW is composed of 2 or more defects with winding numbers

+1/2 or -1/2

Opposite charges annihilate

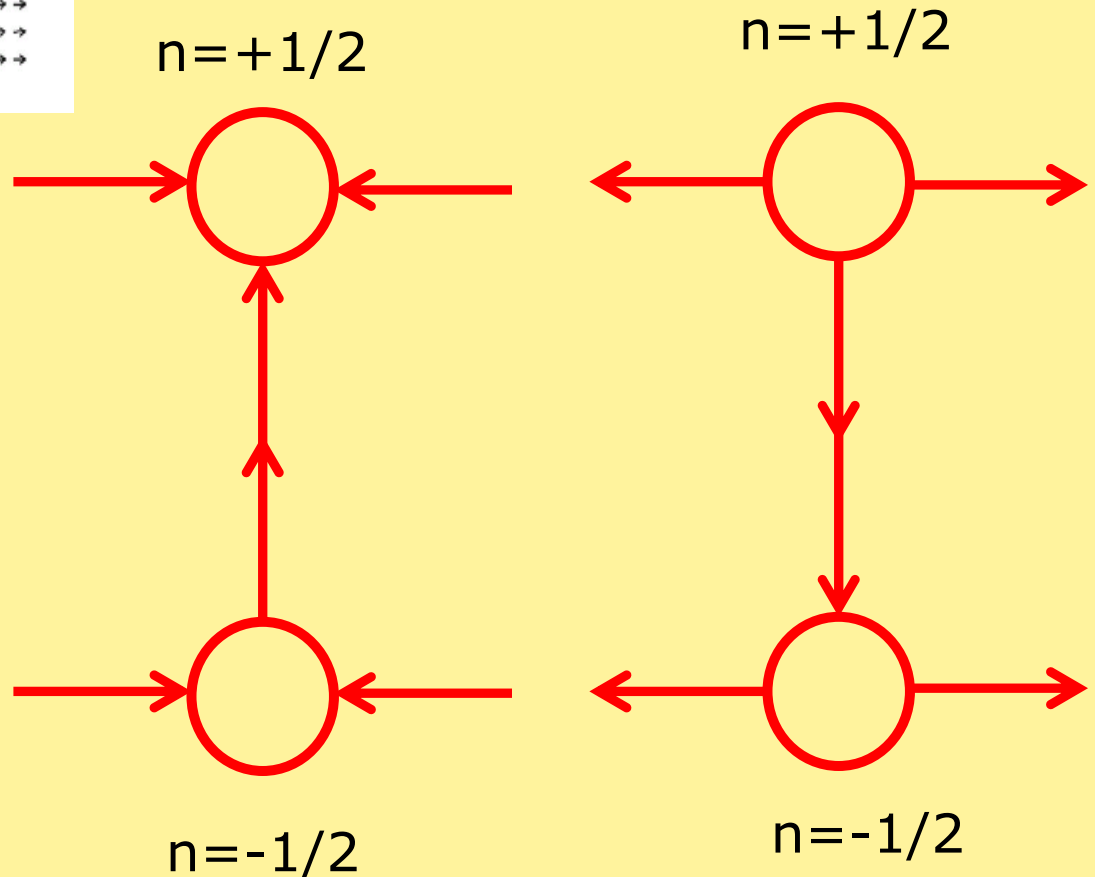
# Edge defects in a domain wall

## II



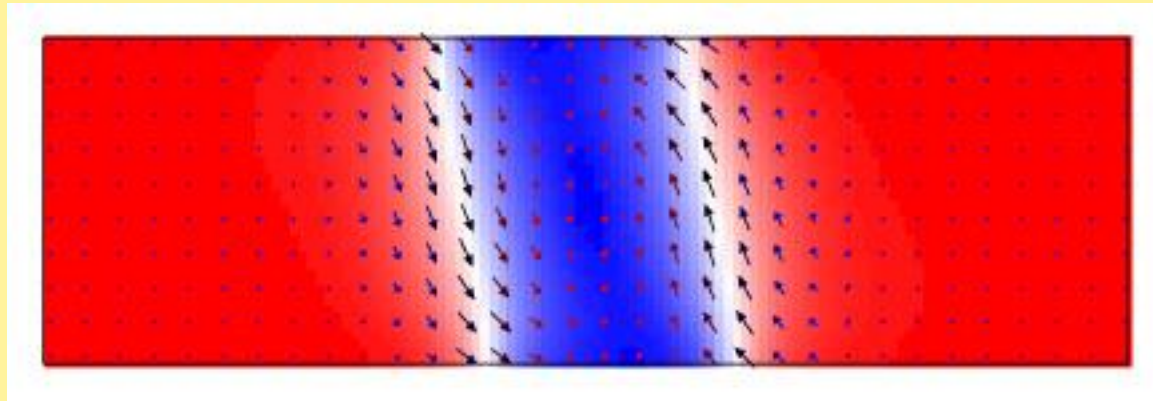
This is a representation of the second stripe (previous slide)

If the total charge on each edge does not add to zero, a 360° wall is formed, and a higher field is necessary to destroy it



Charges do not add to zero

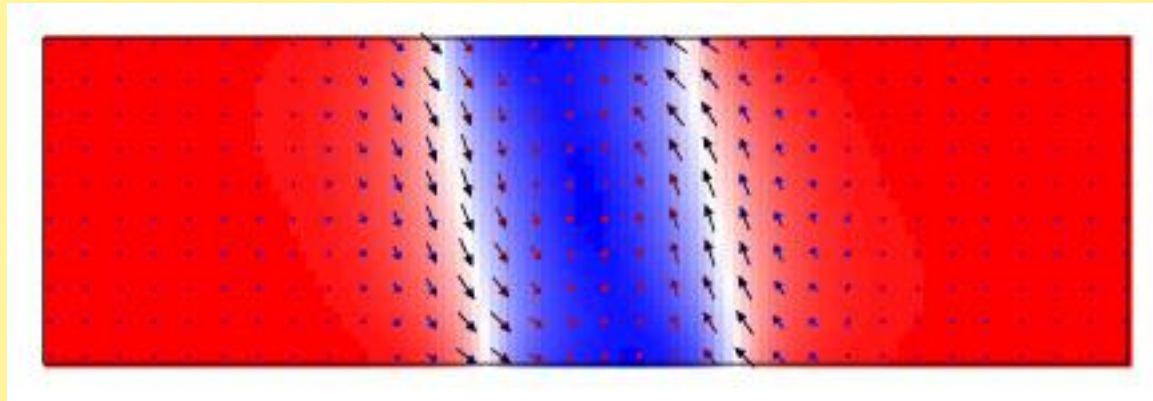
# Collapse of two DWs: formation of a skyrmion 01



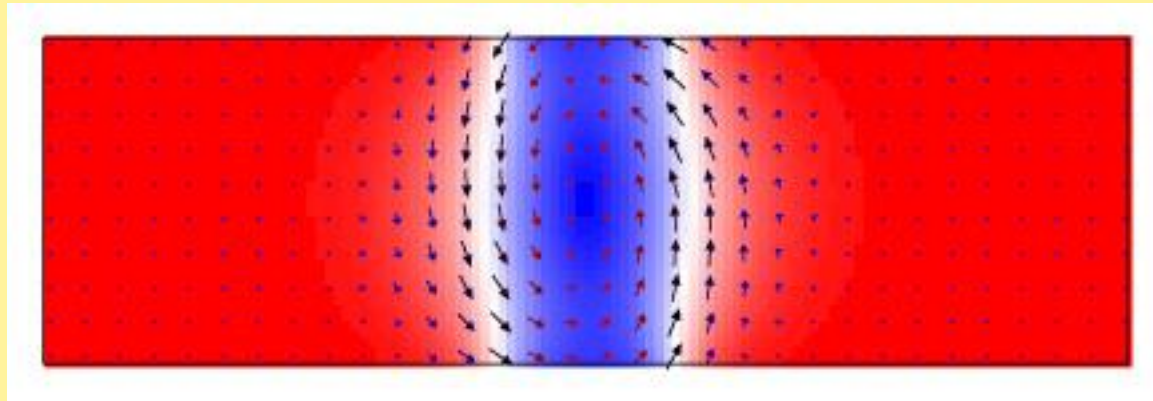
Micromagnetic simulation of a stripe with perpendicular anisotropy, topologically protected, with increasing perpendicular applied field

Garcia, unpublished (2013)

# Collapse of two DWs: formation of a skyrmion 01

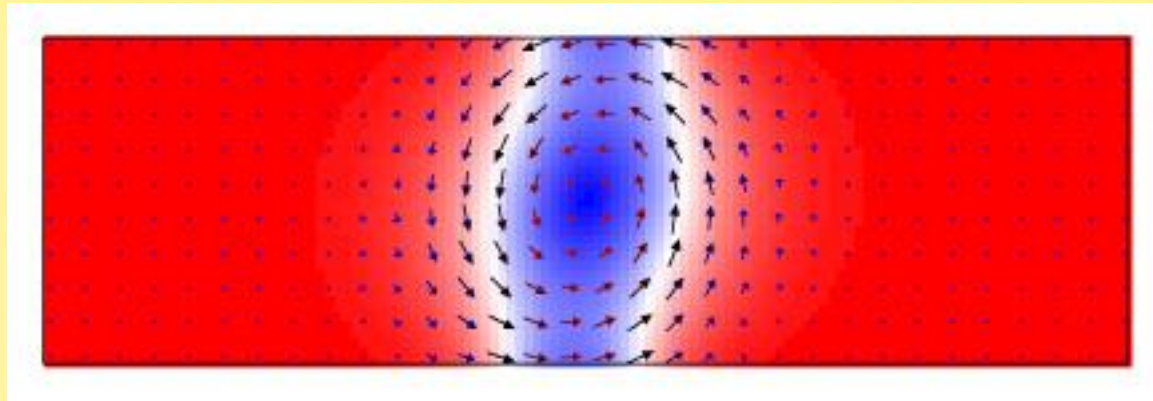


# Collapse of two DWs: formation of a skyrmion 02

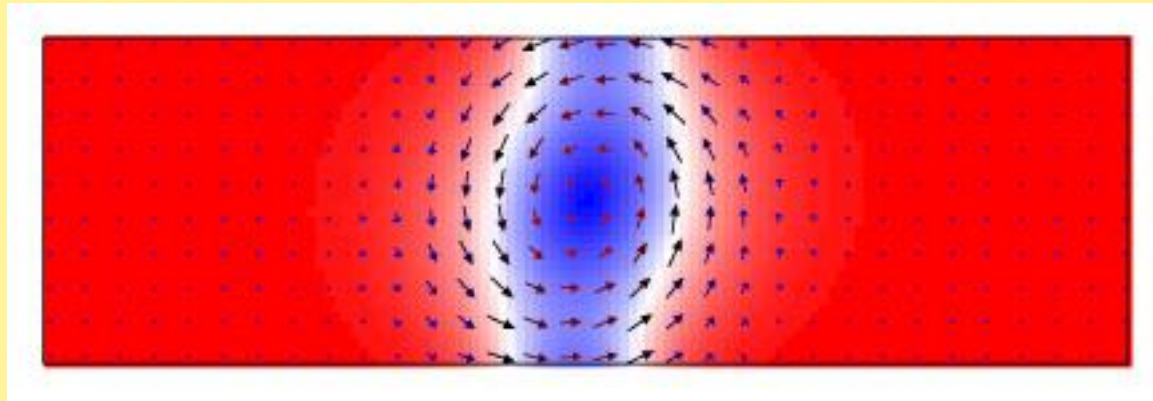




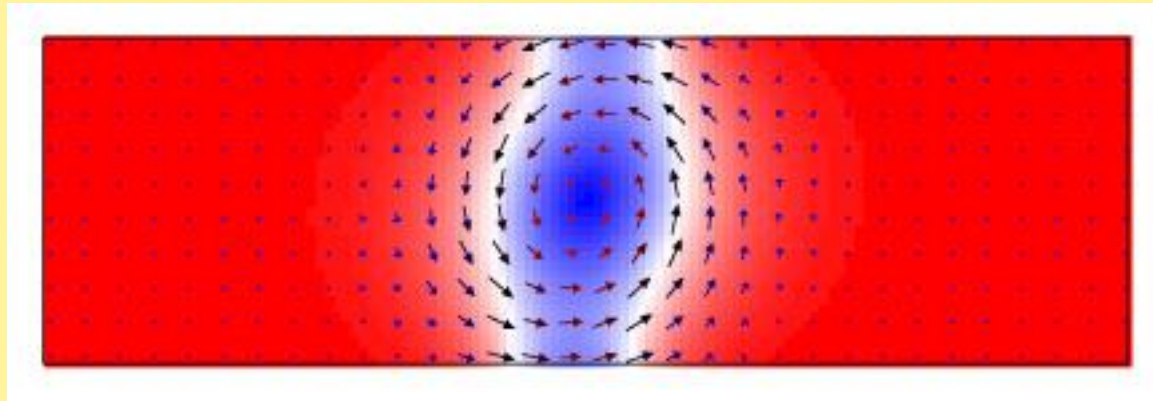
# Collapse of two DWs: formation of a skyrmion 03



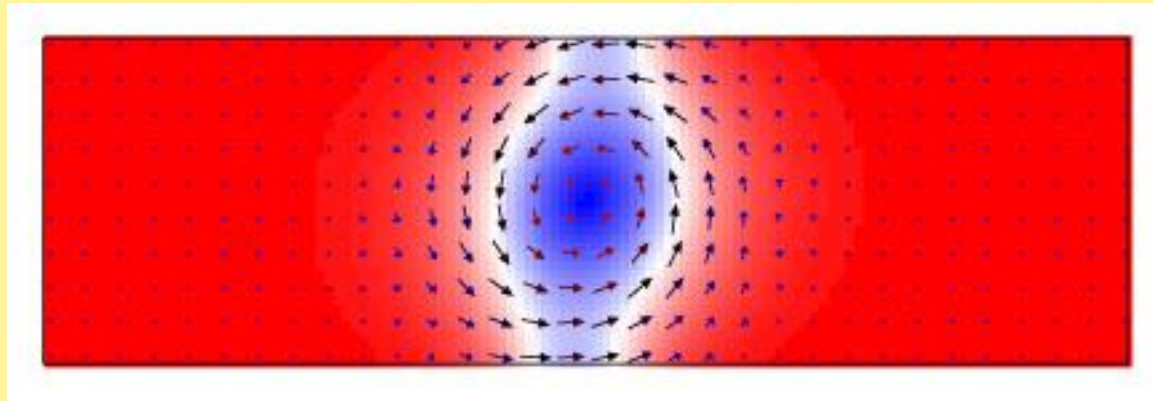
# Collapse of two DWs: formation of a skyrmion 04



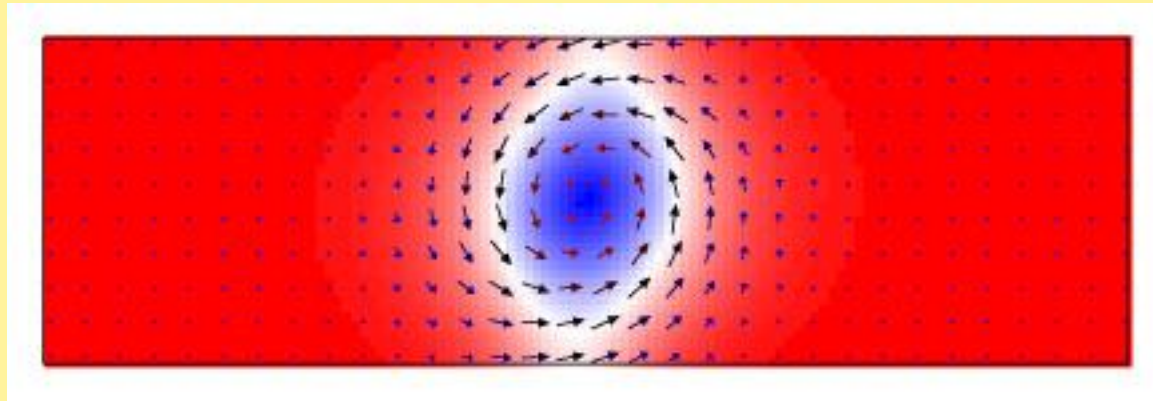
# Collapse of two DWs: formation of a skyrmion 05



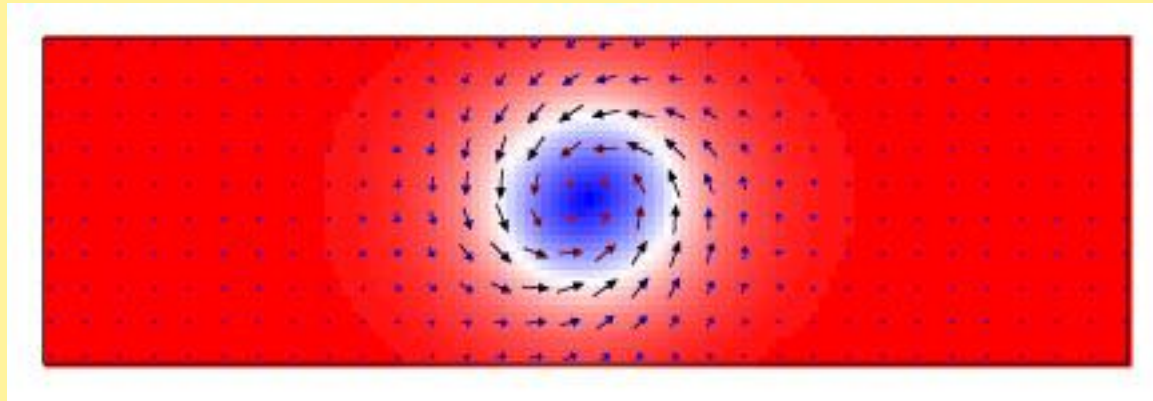
# Collapse of two DWs: formation of a skyrmion 06



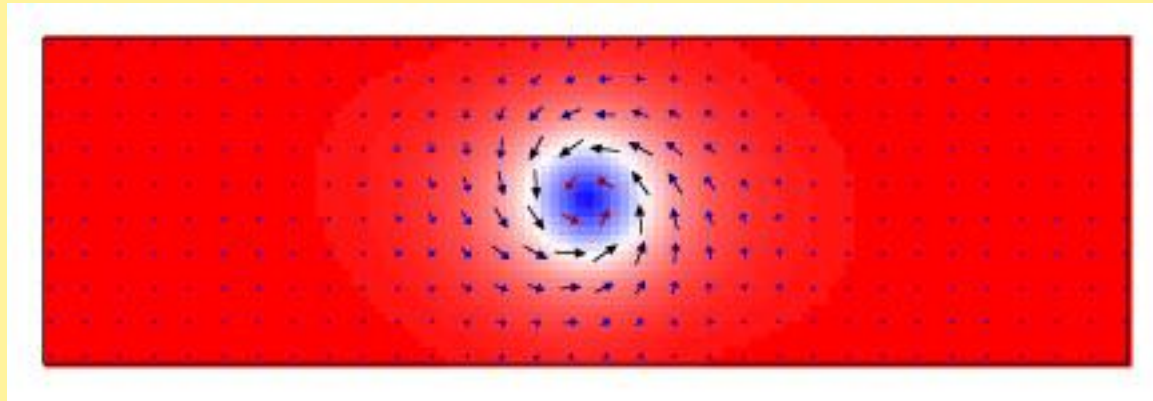
# Collapse of two DWs: formation of a skyrmion 07



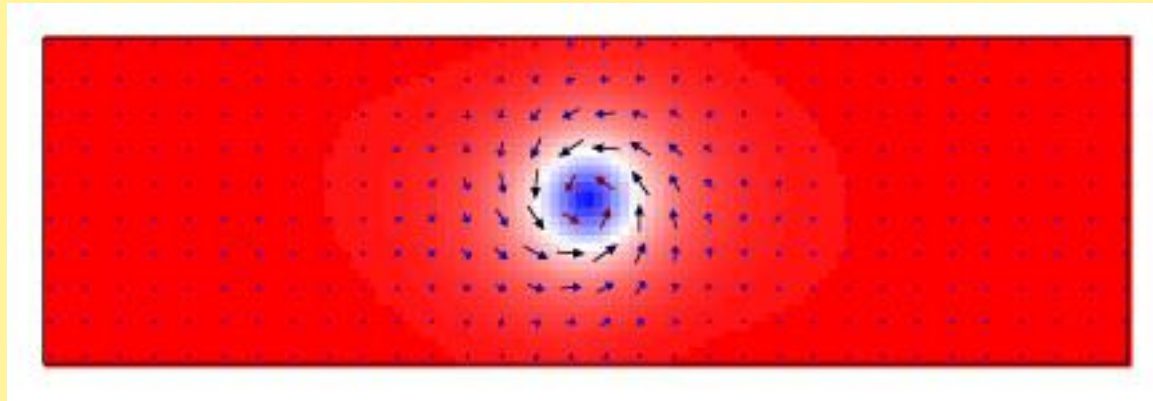
# Collapse of two DWs: formation of a skyrmion 08



# Collapse of two DWs: formation of a skyrmion 09



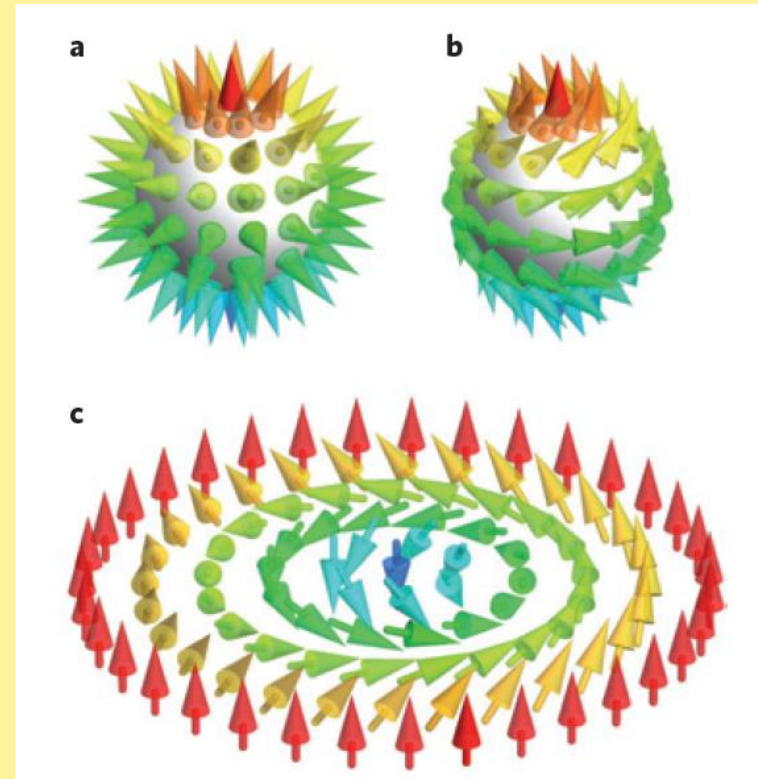
# Collapse of two DWs: formation of a skyrmion 10





# Skyrmions

A class of solitons found in liquid crystals, Bose-Einstein condensates, quantum Hall magnets, thin magnetic films, and materials with Dzyaloshinsky-Moriya (DM) interaction, named after T.H.R. Skyrme (1922–1987)

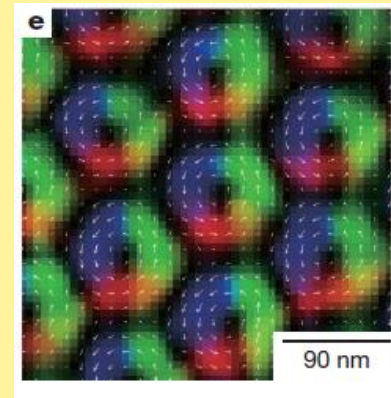


T.H.R. Skyrme, Nucl. Phys. 31, 556–569 (1962).

# Skyrmion lattices and isolated skyrmions

Skyrmion lattices:

Nanolayers of materials with intrinsic chirality (cubic helimagnets  $\text{Fe}_{0.5}\text{Co}_{0.5}\text{Si}$  and  $\text{FeGe}$  (Yu (2010, 2011)) and with induced chirality (Fe/W bilayers) Heinze (2011))



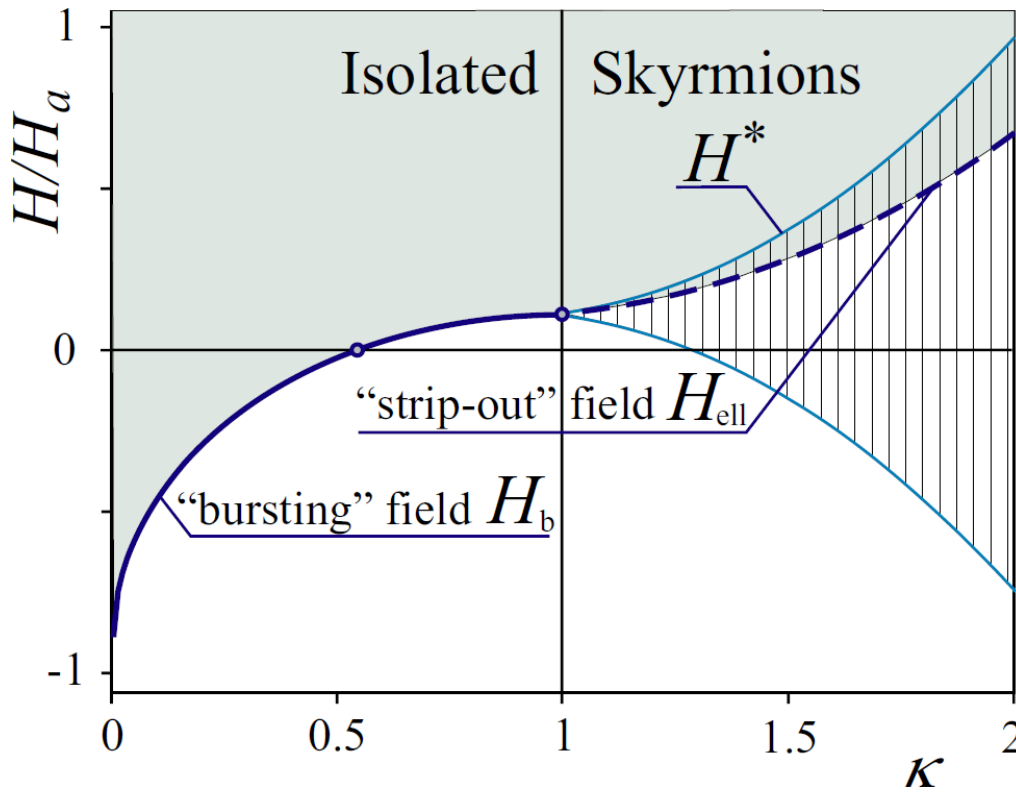
Isolated skyrmions:

Nanolayer of  $\text{Fe}_{0.5}\text{Co}_{0.5}\text{Si}$  ( $L = 20$  nm) for  $H \approx 50$  mT (Yu (2010, 2011)).

Kiselev J. Phys. D: Appl. Phys. 44 (2011) 392001

# Skyrmion phase diagram (Applied field Vs. Kappa)

J. Phys. D: Appl. Phys. **44** (2011) 392001



$$H_a = K/M$$

$$\kappa = \pi D / 4 \sqrt{AK}$$

D – Dzyaloshinsky-Moriya Coefficient

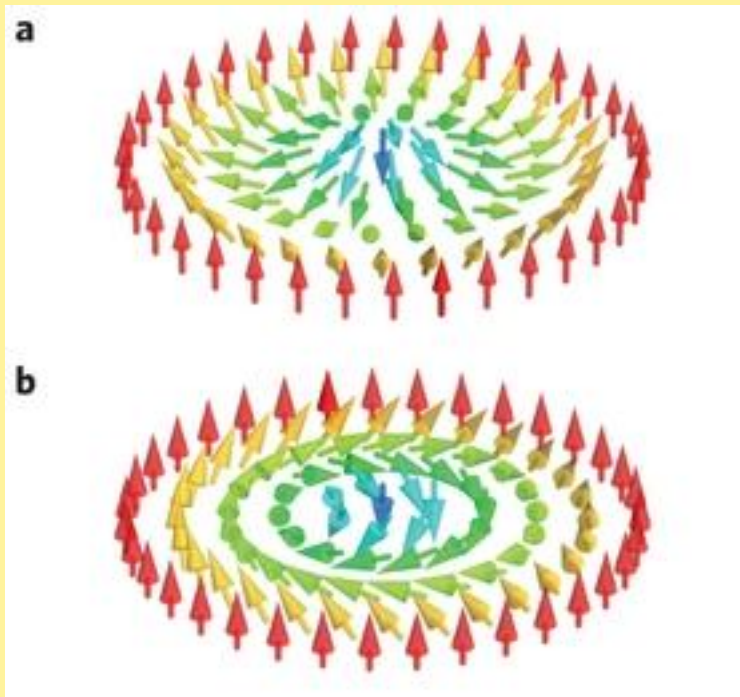
K – anisotropy

A – exchange stiffness

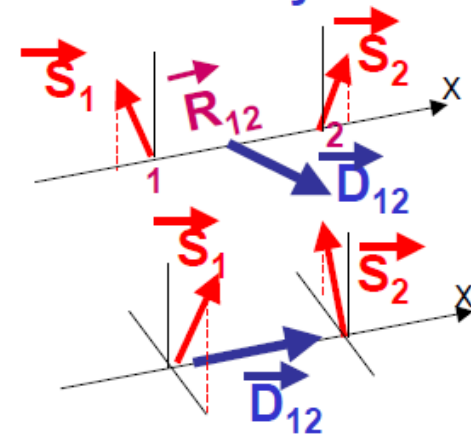
Kiselev J. Phys. D: Appl. Phys. 44 (2011) 392001

Diagram for film of thickness L (fixed ratios  $K/M$  and  $L/W_{DW}$ )  
(in the hatched area spatially modulated skyrmion phases are stable) 43

# Dzyaloshinskii–Moriya interactions



## Dzyaloshinskii-Moriya interactions



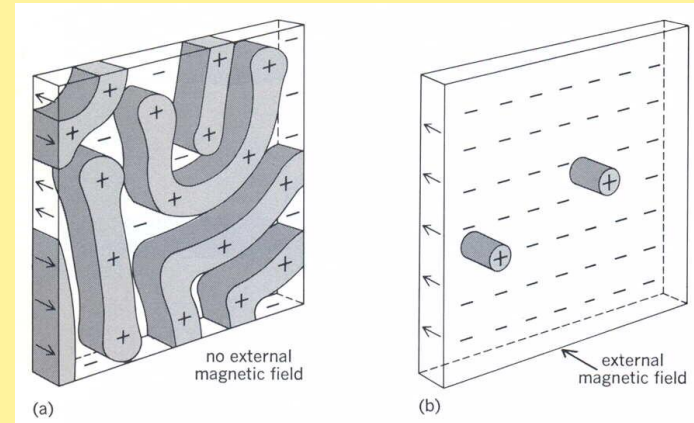
$$H_{DM} = (\vec{S}_1 \times \vec{S}_2) \cdot \vec{D}_{12}$$

# Magnetic bubbles

Cylindrical domains with perpendicular magnetization in magnetic films (e.g., of ferrite, garnet)

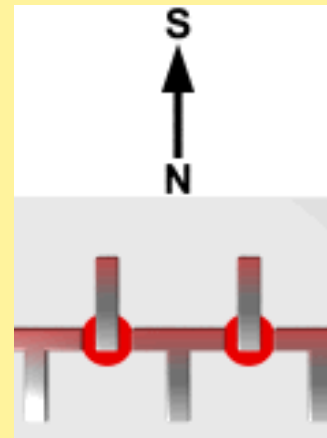
Bubble radius of the order of 1 micron

Applications to magnetic memories studied in the 1960s and 1970s



$H=0$

$H \neq 0$



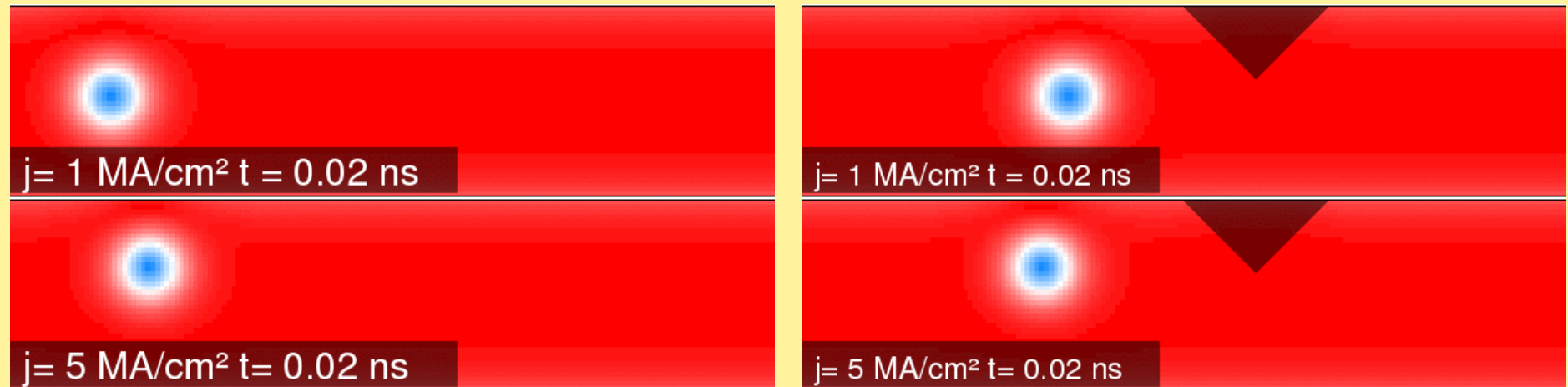
Wikipedia

# Skyrmions on the track

Albert Fert, Vincent Cros and João Sampaio

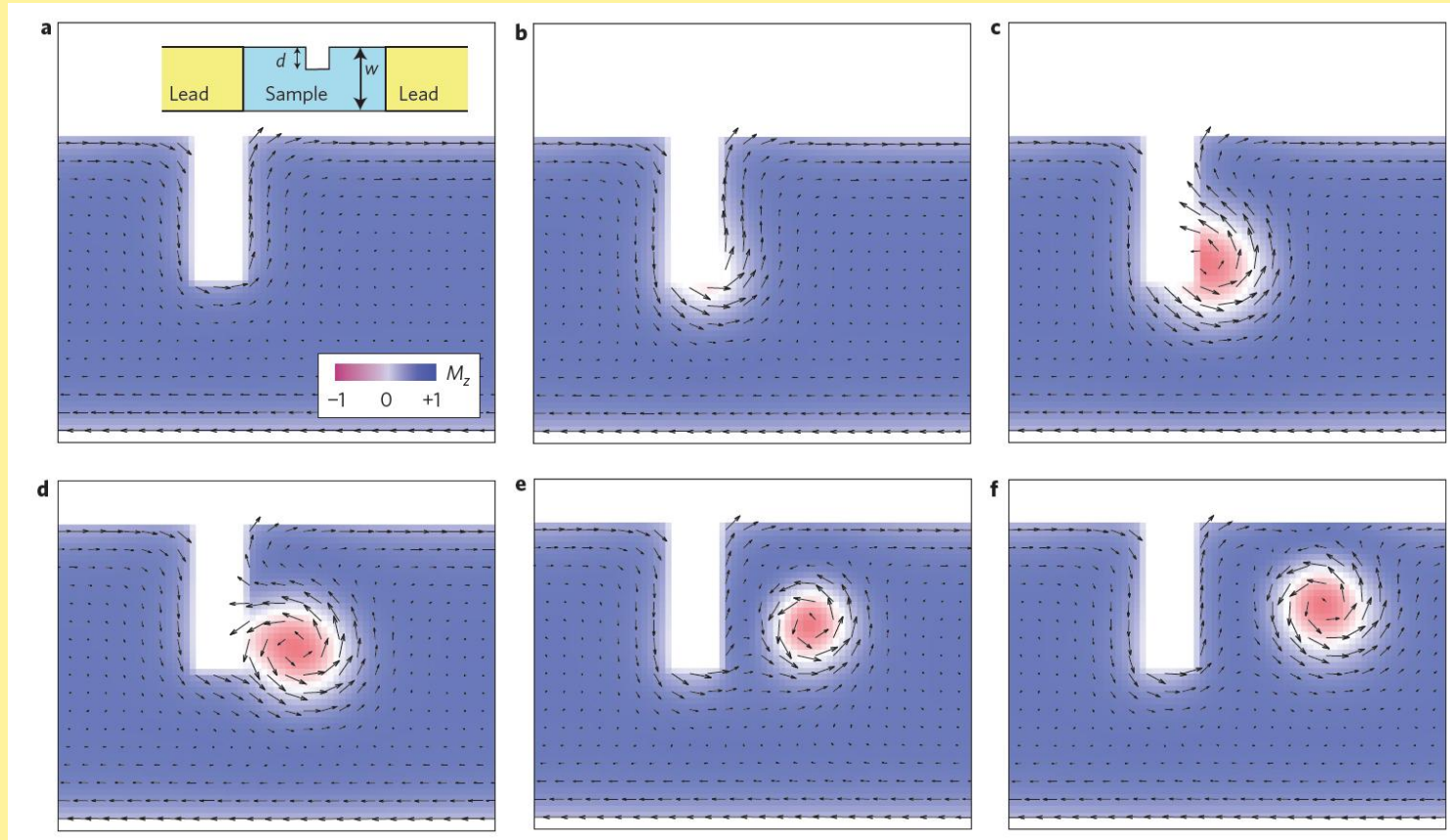
Magnetic skyrmions are nanoscale spin configurations that hold promise as information carriers in ultradense memory and logic devices owing to the extremely low spin-polarized currents needed to move them.

NATURE NANOTECHNOLOGY | VOL 8 | MARCH 2013 |



Current-induced motion of a skyrmion on a Co stripe – low depinning currents

# Creation of skyrmions

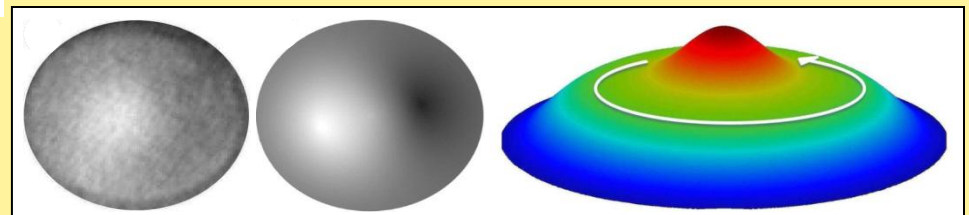
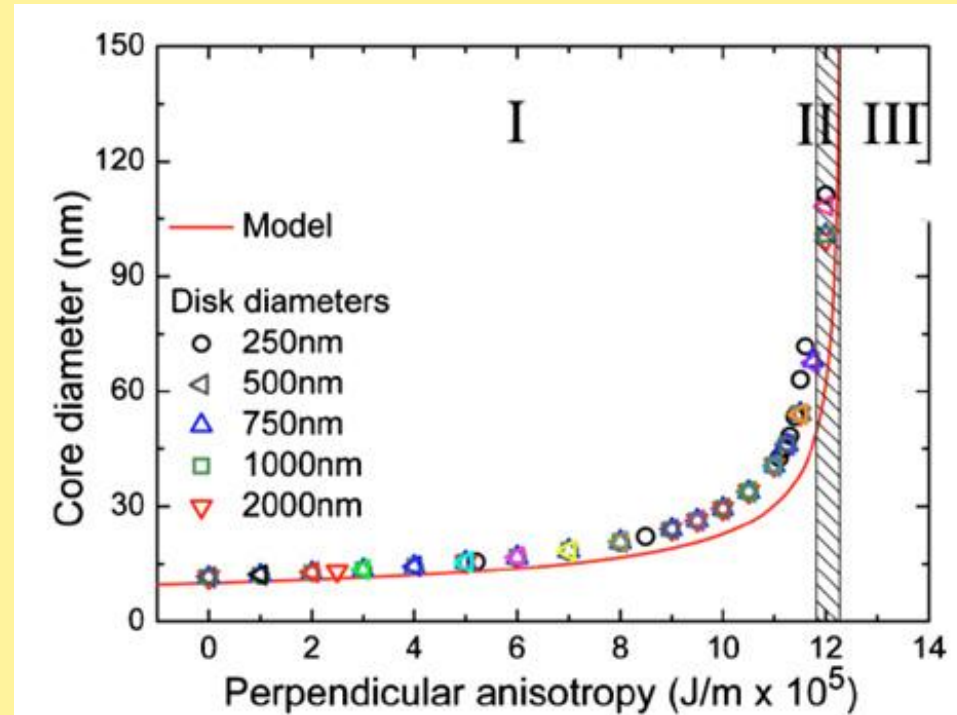
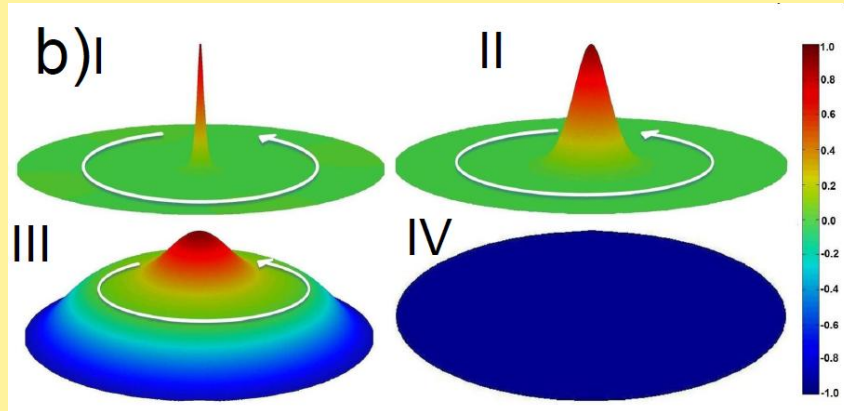


# Tailoring magnetic vortices in nanostructures

F. Garcia,<sup>1,a)</sup> H. Westfahl,<sup>1</sup> J. Schoenmaker,<sup>1</sup> E. J. Carvalho,<sup>1</sup> A. D. Santos,<sup>2</sup> M. Pojar,<sup>3</sup>  
 A. C. Seabra,<sup>3</sup> R. Belkhou,<sup>4,5</sup> A. Bendounan,<sup>4</sup> E. R. P. Novais,<sup>6</sup> and  
 A. P. Guimarães<sup>6</sup>

Tuning the properties of the vortex:

Varying the Co thickness in Co/Pt multilayers, the anisotropy  $K_z$  can be increased, and the vortex core diameter also increases.



1

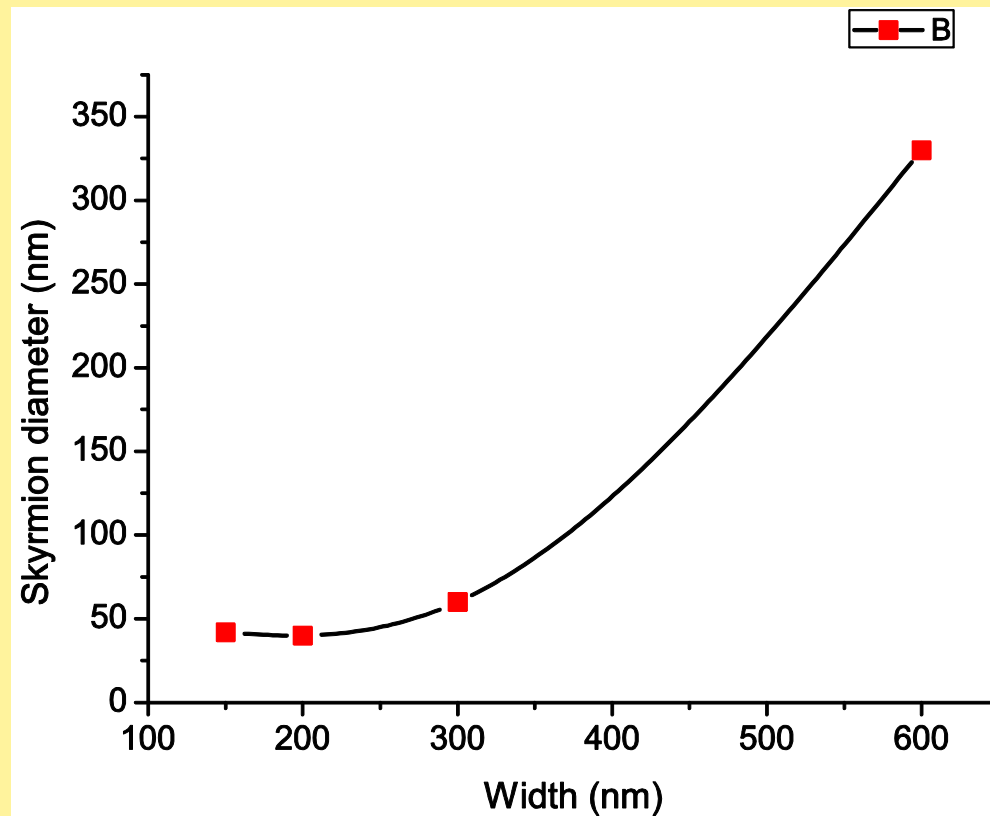
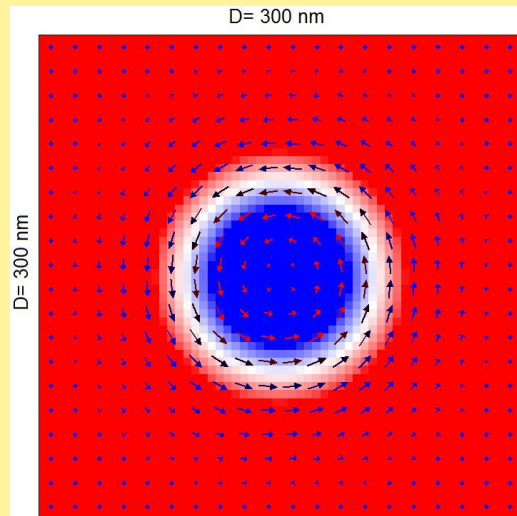
2

3

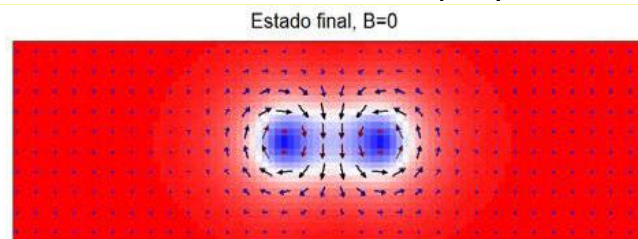
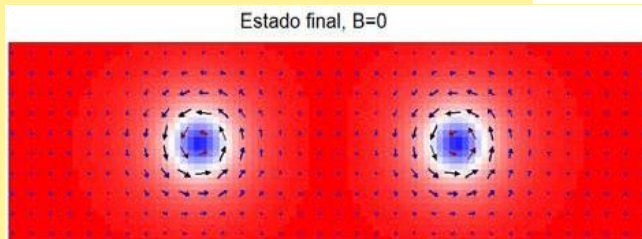
1. PEEM image, 2. simulation, 3. simulation



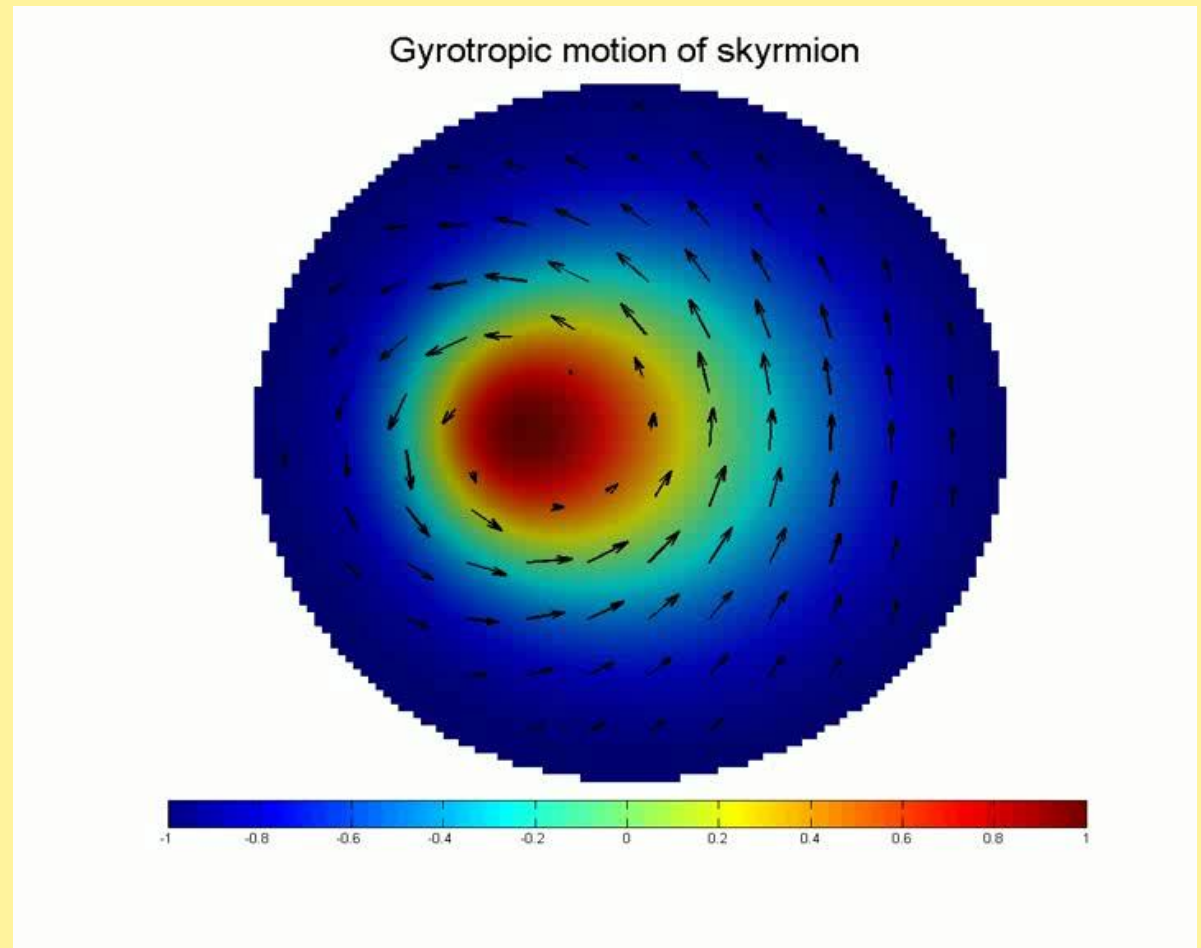
# Skyrmions without DM



Diameter vs. stripe width



# Motion of a skyrmion



Simulation of the motion of a skyrmion in a CoPt disk, with perpendicular anisotropy  $K_z = 1.2 \times 10^6 \text{ J/m}^3$

Novais, unpublished (2013)

# Summary

Topological properties of magnetic systems are relevant for their dynamic behavior

Magnetic vortices and skyrmions are topological defects

Skyrmions are stable structures, topologically protected, related to magnetic vortices and to magnetic bubbles

Skyrmions may be stable with or without DM interaction

Skyrmions may be displaced through the action of polarized currents, with much smaller current densities than domain walls

Skyrmions may have applications in memory devices

# Some general References

A. P. Guimarães, Principles of Nanomagnetism, Springer (2009)

K. Y. Guslienko, J. Nanoscience Nanotechnol., 8 2745-2760 (2008)

A.M. Kosevich et al. Phys. Repts. 194, Nos. 3 & 4 117—238 (1990).

Menzel, Thesis, Hamburg University (2011)

Thank you!