

# Time-Resolved Study of Thermal and Electronic Nonlinearities in $\text{Nd}^{+3}$ and $\text{Cr}^{+3}$ Doped Solids

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In ion doped solids there is a nonlinear refractive index  $n_2$  which is due to the polarizability difference  $\Delta\alpha$  between excited and ground states. Thermal Lens effects are also very significant. This work shows that using time resolved Z-scan technique we can distinguish electronic and thermal nonlinearities. We present the first measurements of the  $\Delta\alpha$  of  $\text{Nd}^{+3}$  ion in fluoride glasses and  $\text{Cr}^{+3}$  doped fluoride crystals. For  $\text{SrAlF}_5:\text{Cr}^{+3}$  we measured  $n_2 = (6.6 + 1.7i) \times 10^{-11} \text{cm}^2$  and calculated  $\Delta\alpha = 3.1 \times 10^{-26} \text{cm}^3$  and  $\Delta\sigma = 1.7 \times 10^{-20} \text{cm}^2$ . In  $\text{InSBZnGdN}$  was observed  $\Delta\alpha = 1.6 \times 10^{-26} \text{cm}^3$ . For ZBLAN we could only estimate  $\Delta\alpha < 2 \times 10^{-27} \text{cm}^3$ .

## 1. Introduction

The study of nonlinear properties is particularly important in laser active media because standing waves in laser cavities produce self-focusing, temporal and spatial self-phase modulation and light-induced gratings that cause effects of hole-burning [1]. Thermal effects, like the thermal variation of the refractive index, thermal expansion and thermally induced stress are also very important in solid-state laser design [2]. The nonlinear properties of different ion doped solids have been studied using several techniques. Like in others materials, the Z-scan technique have been shown to be the best technique for the study of ion doped solids where the nonlinearity is usually slow ( $> 10^{-4}$  sec.) allowing the use of time-resolved methods [3-4]. In ion doped solids the nonlinearity originates from the population

of dopante ion metastable state, which has a complex susceptibility different from that of ground state. The real part of nonlinear refractive index is proportional to the polarizability difference  $\Delta\alpha$  between excited and ground states and the imaginary part is proportional to the absorption cross section difference  $\Delta\sigma$  between excited and ground states. This is the Population Lens effect (PL). Most of these solids present nonlinearity whose real part is one order of magnitude greater than the imaginary one.

Usually, part of the excited state decay is non-radiative, so the laser heats the sample and an optical path change is established owing to the temperature coefficient of the optical path,  $ds/dT$ , which causes the so-called Thermal Lens (TL) [5]. In fluoride glasses, usually  $\Delta\alpha$  is very small and it was observed that PL

is smaller than TL effect [7]. In this work, we show that it is possible to temporally distinguish these two effects in  $\text{Nd}^{+3}$  and  $\text{Cr}^{+3}$  doped solids.

When the ion doped solid is pumped in resonance with an absorption line, both thermal and electronic nonlinearities are proportional to the ion excited state population  $N_{ex}(t)$  which time evolution can be calculated using rate equations [6]:

$$N_{ex}(t) = N_0 \frac{(1 - e^{-t/\tau})I/I_s}{(1 + I/I_s)} \quad (1)$$

with

$$\tau^{-1} = \tau_0^{-1}(1 + I_0/I_s) \quad (2)$$

where  $I$  is the laser intensity,  $N_0$  is the total ion concentration,  $I_s = \hbar\omega/\sigma\tau_0$  is the saturation intensity,  $\hbar\omega$  is the pump photon energy,  $\sigma$  is the absorption cross section and to the lifetime. The complex refractive index can be written as  $n(t) = n_0 + \Delta n(t)$ , where  $\Delta n$  is the laser induced variation due to PL or TL effects. The intensity dependence of the sample trough an aperture in the far field is proportional to the phase shift  $\Delta\phi = (2\pi/\lambda)\Delta nL$ , where  $L$  is the sample thickness.

First we consider the TL effect, where the phase shift is given  $\Delta\phi_{th}$ :

$$\Delta\phi_{th} = \frac{PAL}{K\lambda_p} \varphi \frac{ds}{dT} \quad (3)$$

where  $P$  is the excitation laser power,  $A$  is the absorption coefficient,  $K$  is the thermal conductivity,  $\lambda_p$  is the probe beam wavelength,  $L$  is the sample length and  $\varphi$  is the fraction of absorbed energy converted into heat per photon. If the sample fluorescence quantum efficiency is  $\eta$ ,  $\lambda_{ex}$  is the excitation beam wavelength,  $\lambda_{em}$  is the average emission wavelength, then  $\varphi = (1 - \eta\lambda_{em}/\lambda_{ex})$ . In the case of the  $\text{Nd}^{+3}$  ion,  $\lambda_{ex} \sim 0.5 \mu\text{m}$  and  $\lambda_{em} \sim 1.06 \mu\text{m}$  and  $h\eta \sim 1$  so  $\varphi \sim 0.5$  [8-9]. TL signal response time is given by:

$$t_c = w^2/4D \quad (4)$$

where  $D = K/\rho C$  is the thermal diffusivity,  $\rho$  is the density,  $C$  is the specific heat and  $w$  is the excitation beam radius.

The PL refractive index variation is given by  $\Delta n_p = n_2 I$ , then the PL phase shift can be written as:

$$\Delta\phi_{pop} = (4\pi^2 f_L^2/\lambda n_0)\Delta\alpha L N_0 I_0/I_s \quad (5)$$

where  $f_L = (n_0^2 + 2)/3$  is the Lorentz local field correction factor,  $n_0$  is the real part of the linear refractive index,

$\Delta\alpha$  is the polarizability difference between excited and ground states of the dopant ion,  $I_0 = 2P/\pi w_0^2$ , is the on axis intensity of the gaussian  $\text{TEM}_{00}$  profile and  $w_0$  is the beam radius at focus.

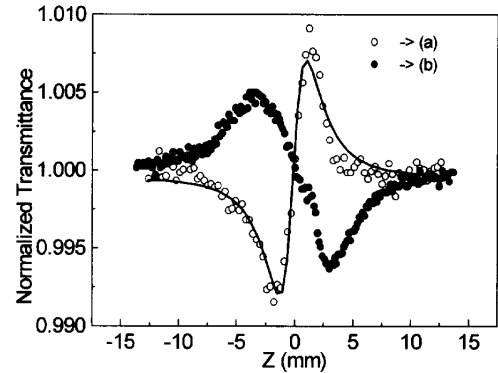


Figure 1. Time-resolved Z-scan of  $\text{Nd}^{+3}$  doped fluorinate glass where curve (a) shows data for chopper frequency  $f = 840$  Hz and laser power  $P = 0.187$  W and curve (b) shows data for  $f = 90$  Hz,  $P = 0.23$  W.

The Fig.1 shows our time-resolved Z- scan data performed at two different chopper frequencies in order to discriminate PL and TL effects in  $\text{Nd}^{+3}$  doped  $\text{InSbZnGdN}$  fluorinate glasses [7]. In this experiment the PL effect is faster than TL, so at high chopper frequency the characteristic Z-scan curve for positive nonlinearity was observed and attributed to PL effect. The PL curve shown is already normalized by the open aperture Z-scan ( $S_1=100\%$ ) as usually done in this technique. The open aperture data ( $S_1=100\%$ ) indicates a small absorption, so the complex  $n_2$  is  $(1.1 - 0.05i)10^{-10} \text{ cm}^2/\text{W}$ . At lower chopper frequency the curve is inverted indicating  $\Delta n < 0$  and consequently  $ds/dT < 0$ , as usually observed in fluoride glasses. The distance between peak and valley is doubled ( $\Delta T_{pv} \sim 3.4z_0$ ) as expected for a TL Z-scan[7]. From our PL data, we calculated  $\Delta\alpha \sim 1.6 \cdot 10^{-26} \text{ cm}^3$ .

For ZBLAN and in both chopper frequencies we always observed  $\Delta n < 0$ . This indicates that either  $n_2 < 0$  or the PL effect is too small compared to the TL one. Therefore we could only estimate  $\Delta\alpha < 2 \times 10^{-27} \text{ cm}^3$ . In the sample YAG we obtained  $n_2 = 1.4 \times 10^{-10} \text{ cm}^2/\text{W}$  and  $\Delta\alpha = 4.1 \times 10^{-26} \text{ cm}^3$ .

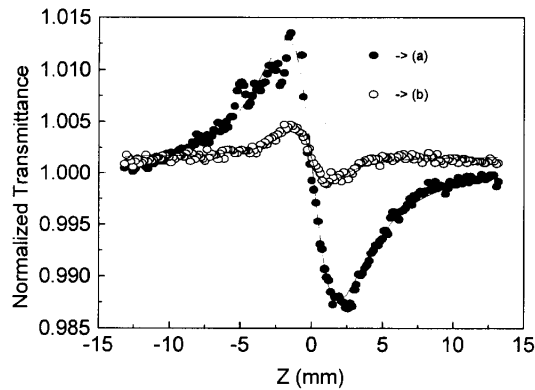


Figure 2. Normalized Transmittance obtained in ZBLAN sample. The curve (a) shows data for  $f = 186\text{Hz}$  and curve (b) shows data for  $f = 824\text{Hz}$ . Both curves shows  $n_2 < 0$ .

The Fig.3 shows our results open ( $S_1$ ) and closed-aperture ( $S_2$ ) data, to  $\text{SrAlF}_5:\text{Cr}^{+3}$  at high frequency. The open-aperture data present a decrease in transmittance near the focus due to a excited state absorption. The division curve indicates a positive nonlinearity with  $n_2 = 6.6 \times 10^{-11} \text{ cm}^2/\text{W}$  and using Eq. (5) we calculated  $\Delta\alpha = 3.1 \times 10^{-26} \text{ cm}^3$ . The Fig.4 shows our Z-scan data lower frequency. In this case, the closed aperture curve indicate a negative nonlinearity, which was attributed to TL effect. This curve can be fit with theoretical thermal lens model [5] where we obtained  $D$  which is used to calculate the thermal diffusivity  $D = 6.5 \times 10^{-3} \text{ cm}^2/\text{s}$ .

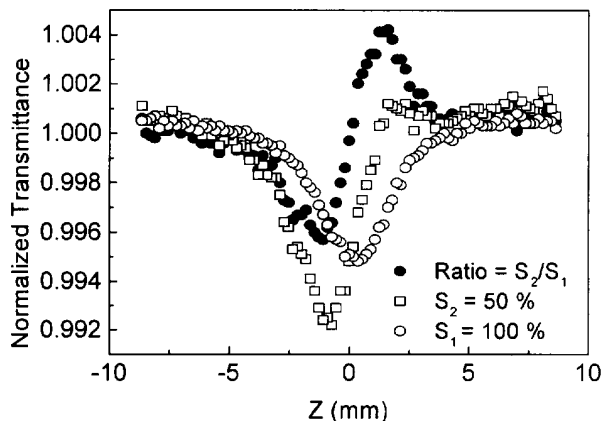


Figure 3. Normalized Transmittance obtained in  $\text{SrAlF}_5:\text{Cr}^{+3}$  sample for laser power  $P = 0.09\text{W}$  and frequency  $f = 822 \text{ Hz}$ .

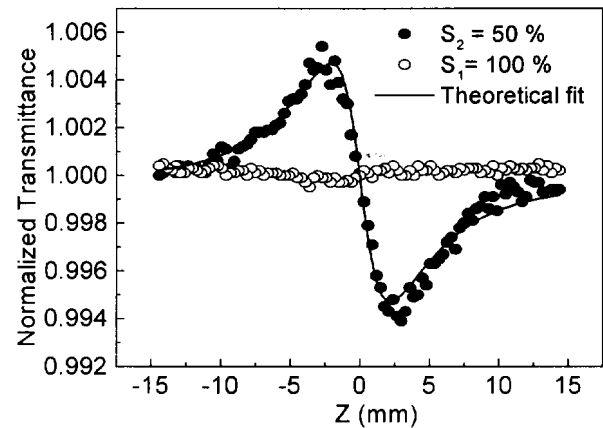


Figure 4. Normalized Transmittance obtained in  $\text{SrAlF}_5:\text{Cr}^{+3}$  sample with  $P = 0.175\text{W}$  and  $f = 186 \text{ Hz}$ .

In this work, we have shows that even when  $\Delta\phi_{th} > \Delta\phi_{pop}$  these two effects can be distinguished temporally by measuring with appropriate chopper frequencies. The same procedure has been used before to distinguish the nonlinear effect of the two different sites of  $\text{Cr}^{+3}$  in alexandrite [6].

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